

# Understanding Ecosystem Productivity and Predicting Population Resilience Via Steepness

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# Overview

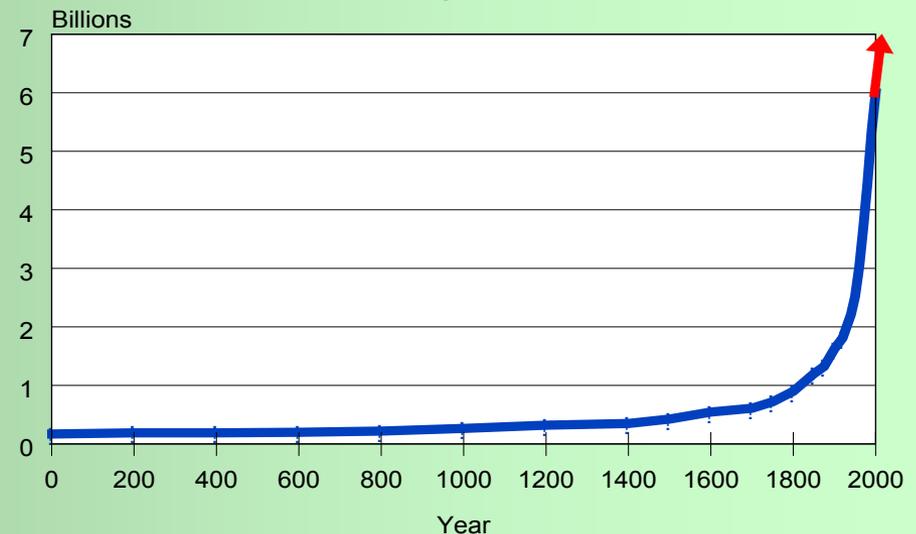
- **BACKGROUND**
  - **EXAMPLE: NORTH PACIFIC STRIPED MARLIN**
  - **CONCLUSIONS AND FUTURE RESEARCH**
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- A North Pacific Striped Marlin is shown swimming underwater. The fish is dark-colored with a lighter stripe along its side. It has a long, pointed snout and a large dorsal fin. The background is a deep blue, suggesting an underwater environment.

# An Ecosystem Approach to Management

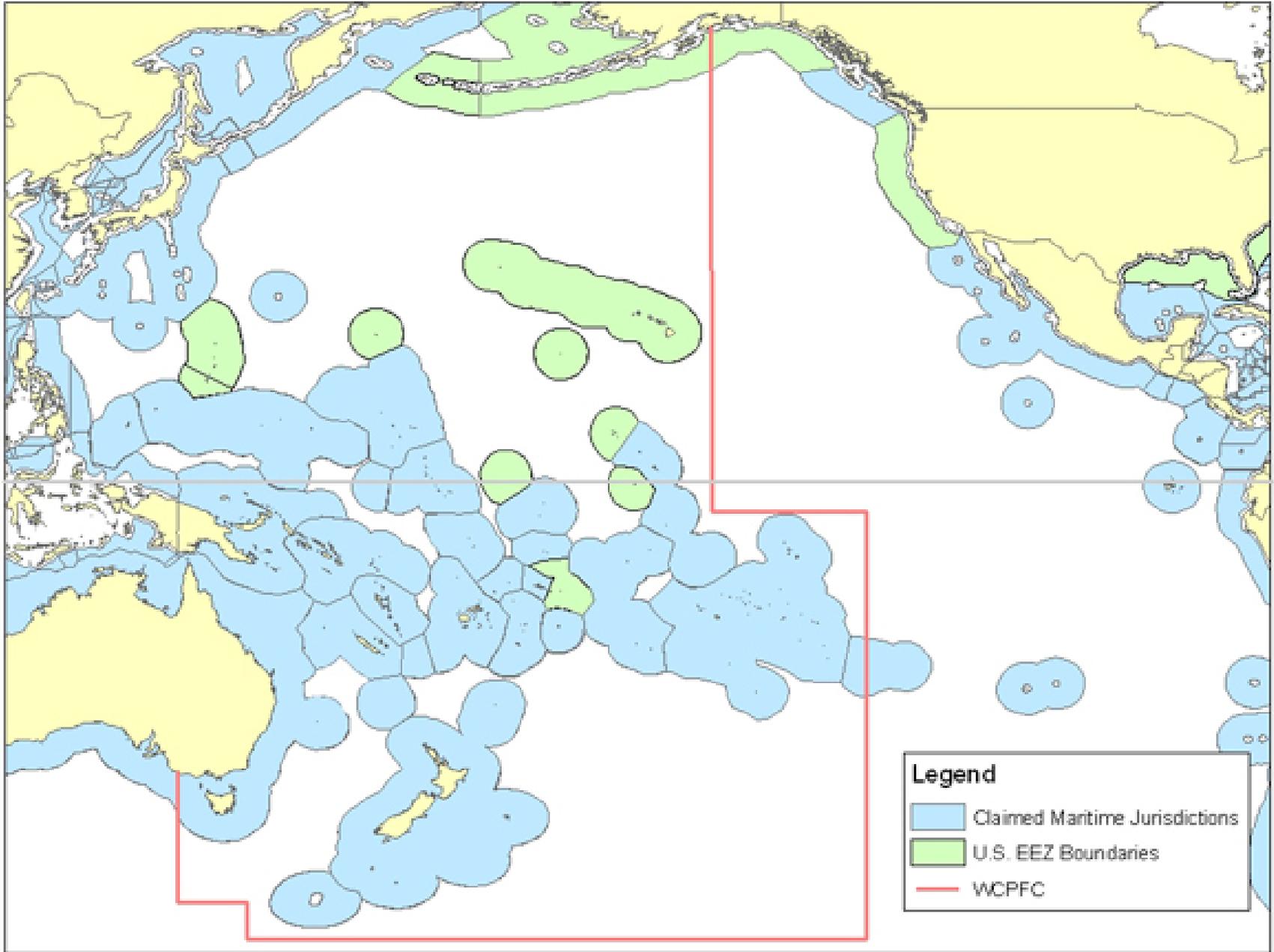


- Monitor ecological indicators of ecosystem status
  - Assess status of fisheries resources
  - Provide forecasts for fisheries resources and for the marine ecosystem
- 
- What are the effects of fishing ?
  - What are the impacts of environmental change ?

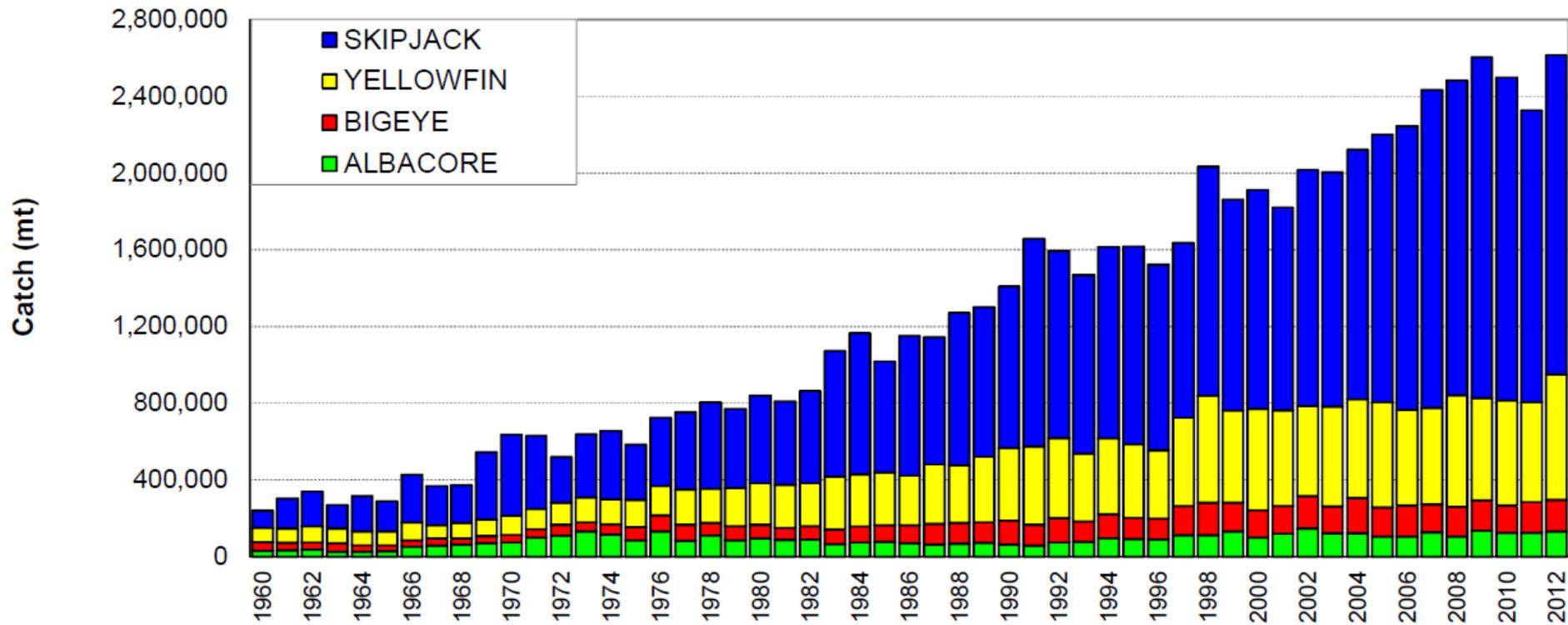
Human Population Size



# Western and Central Pacific Fisheries Commission



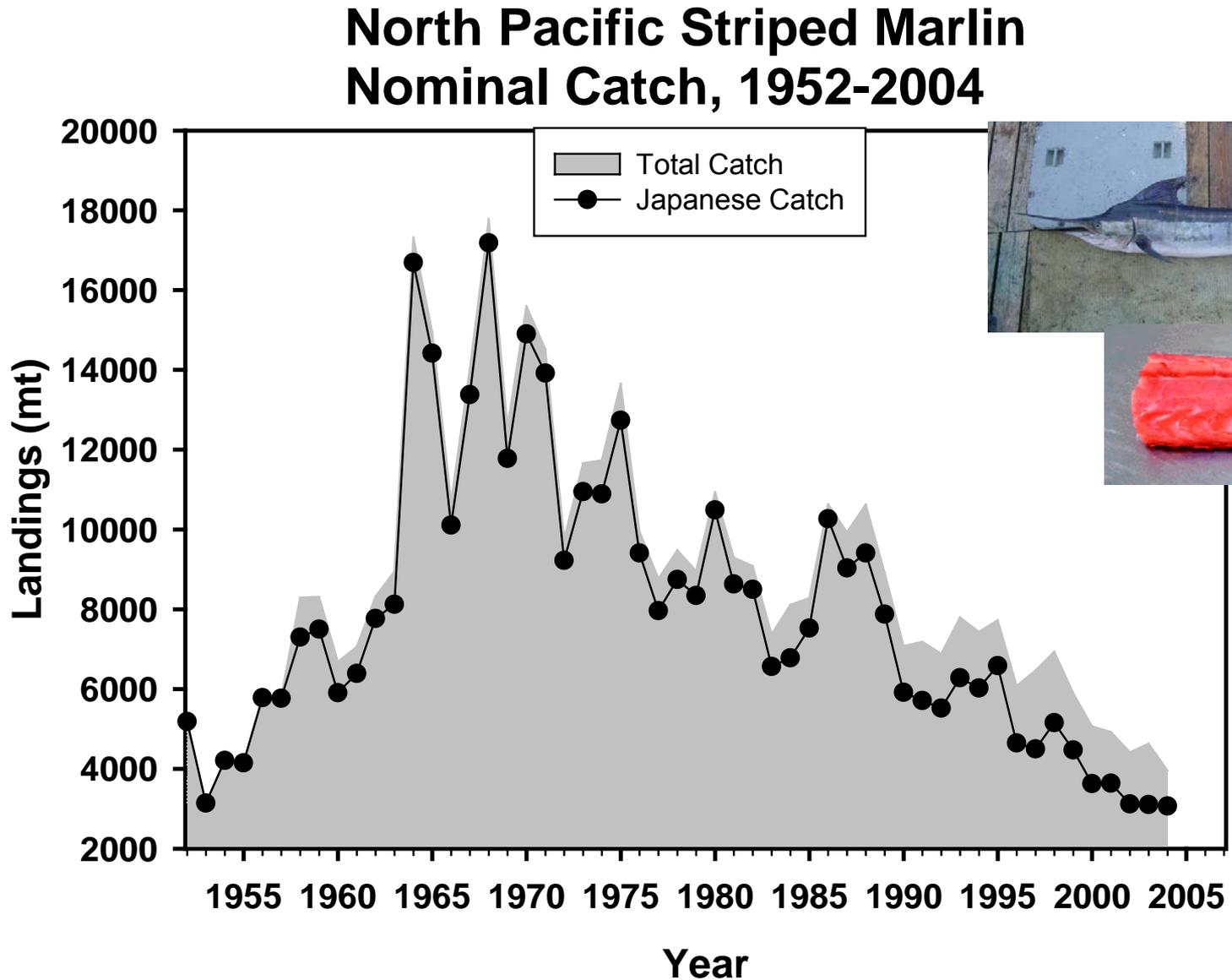
# Western and Central Pacific Pelagic Fisheries: Trends in Catch by Species



Probably all the great sea fisheries  
are inexhaustible” ~ Thomas Huxley 1884

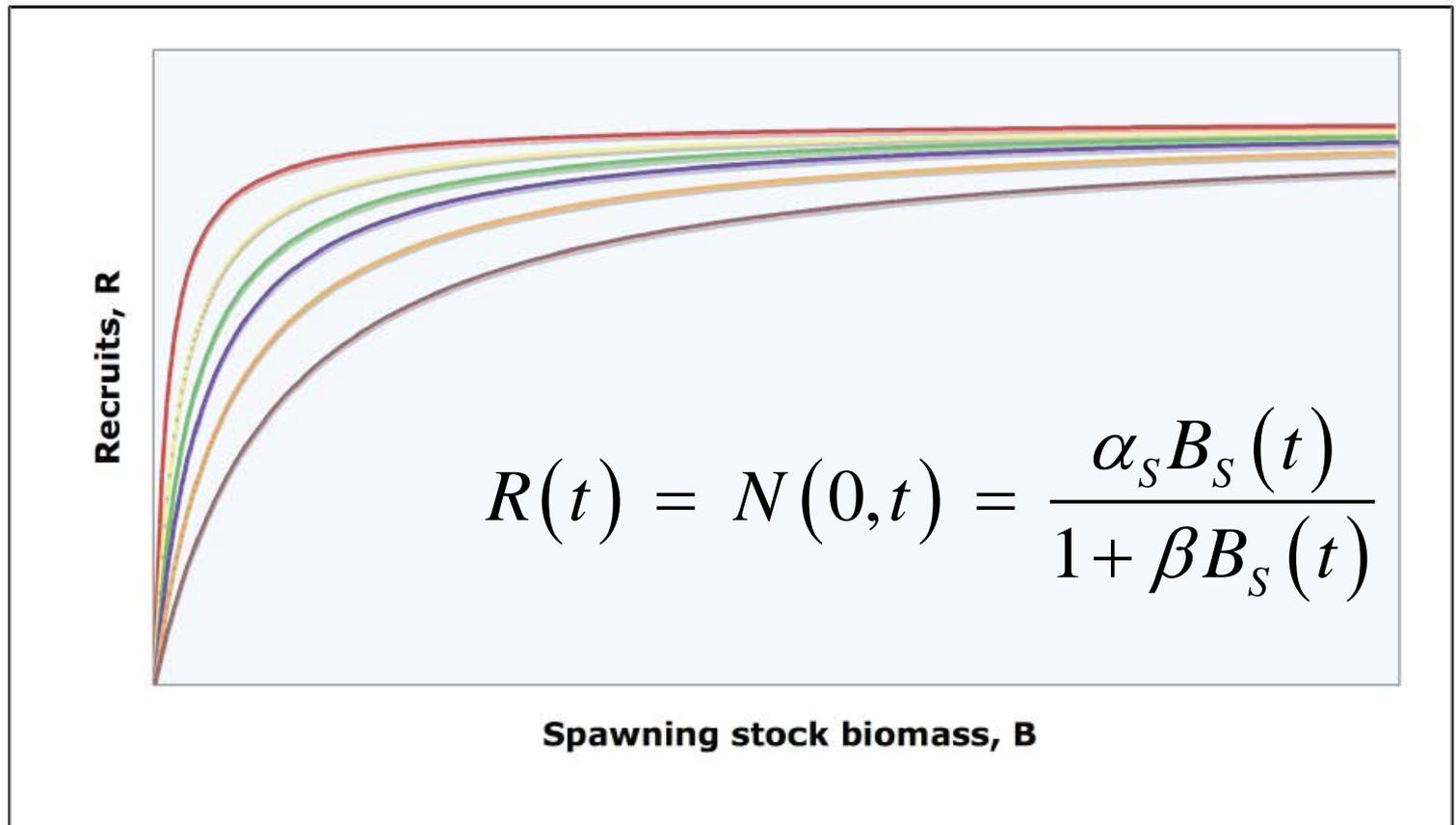
“It is a mistake to suppose that  
the whole ocean is practically  
one vast store house”  
~ Ray Lankester 1884

# North Pacific Striped Marlin Assessment in 2007: A One-Way Trip



# Classical Approach to Density-Dependent Recruitment

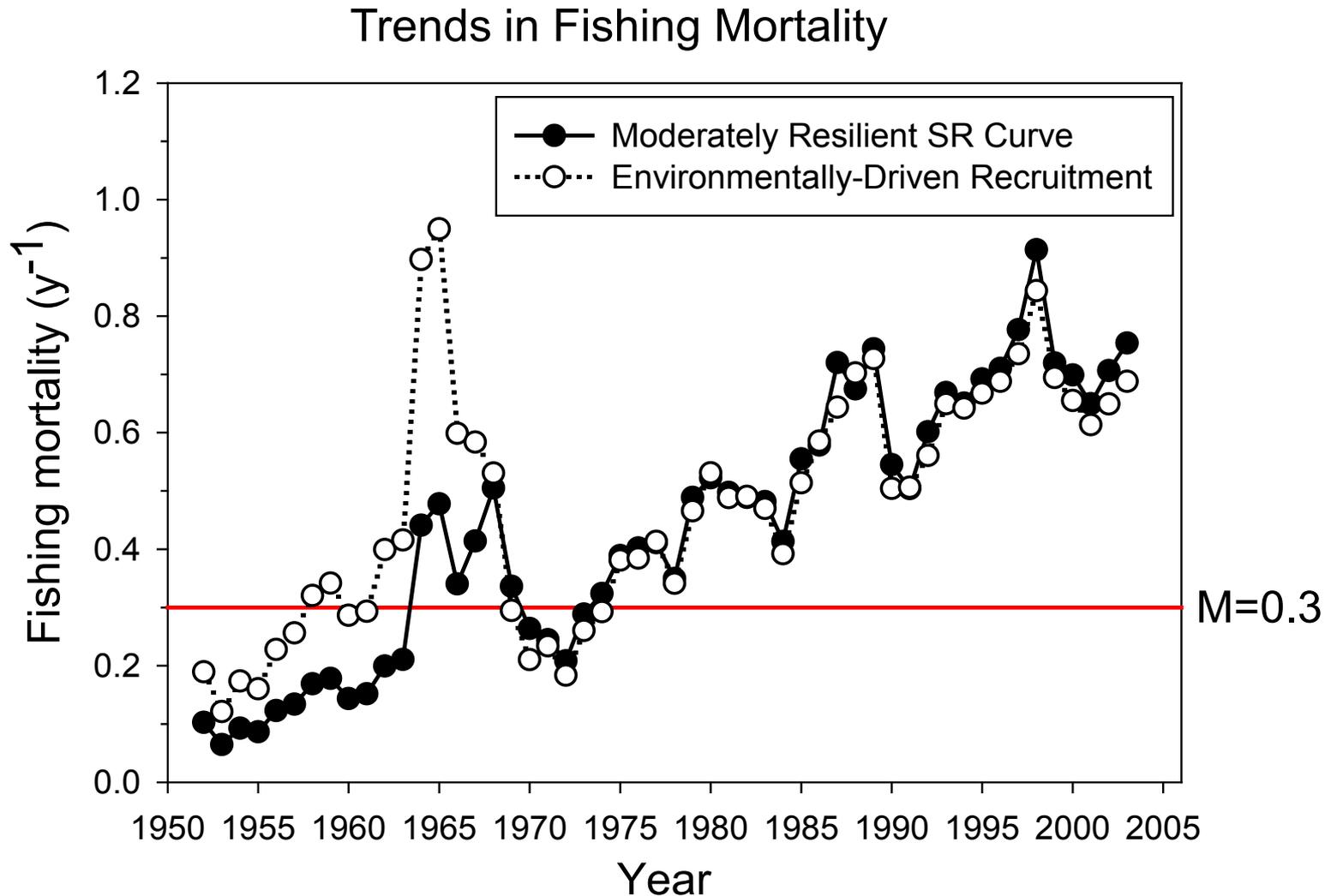
$$R = f(B)$$



$B_s(t)$  is mature female biomass at time  $t$

# Uncertainty About Resilience

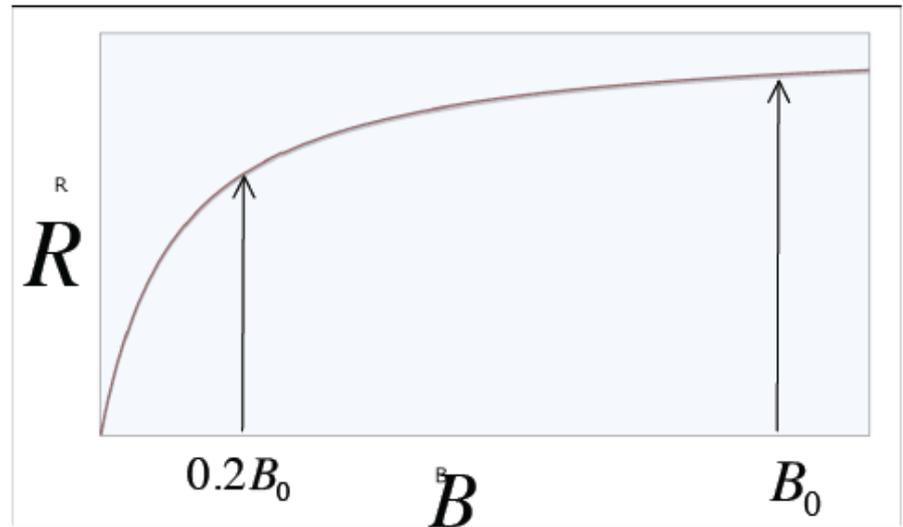
- **Recruitment dynamics modeled using 2 hypotheses**
  - Mean recruitment follows a Beverton Holt SR curve,  $h=0.7$
  - Environmentally-driven recruitment about mean,  $h=1$



## What is Steepness: Mace and Doonan (1988)

Steepness: Fraction of the recruitment at the unfished the spawning biomass when the spawning biomass is 20% of the unfished size

$$h = \frac{R(0.2B_0)}{R(B_0)}$$



Mace, P. and I.J. Doonan. 1988. A Generalised Bioeconomic Simulation Model for Fish Population Dynamics. New Zealand Fishery Assessment Research Document 88/4, Fisheries Research Centre, MAFFish, POB 297, Wellington, NZ.

# Calculating a Prior Distribution for Steepness

Apply Standard Age-Structured Population Dynamics Model For An Unfished Stock With

- Density-Independent Growth, Maturity, Fecundity
- Beverton-Holt Recruitment Dynamics
- Allometric Scaling of Natural Mortality

**Expected female spawning biomass per recruit**

$$SPR_f = \sum_{a=1}^{A_{MAX}} S(a) \cdot W_f(a) \cdot p_{f,m}(a)$$

# Steepness as a Function of Slope at the Origin

Simplify the expression for steepness ( $h$ ) using lifetime expected female spawning biomass per recruit and Beverton-Holt assumption gives

$$h = \frac{\alpha_S \cdot SPR_f}{4 + \alpha_S \cdot SPR_f}$$

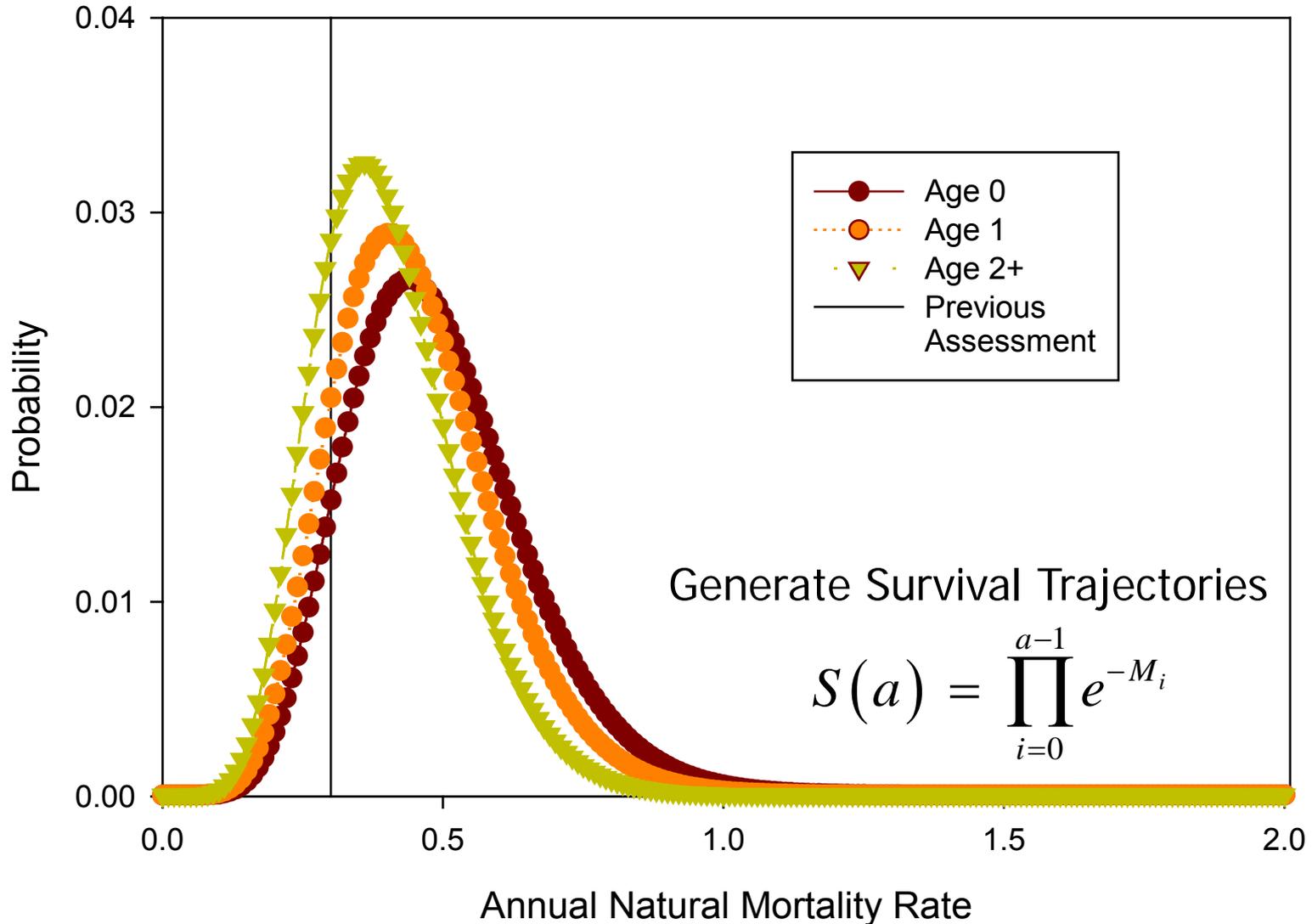
# Monte Carlo Simulation to Construct Steepness Distribution

Randomly sample age distribution of subpopulation  $k$   $\{A_{n,k}\}$  with fish mass  $W(A_{n,k})$ , fecundity  $F(W)$ , early life history survival rate  $S(A_{n,k})$ , and mean number of batches of eggs  $n_B$  to estimate slope at origin

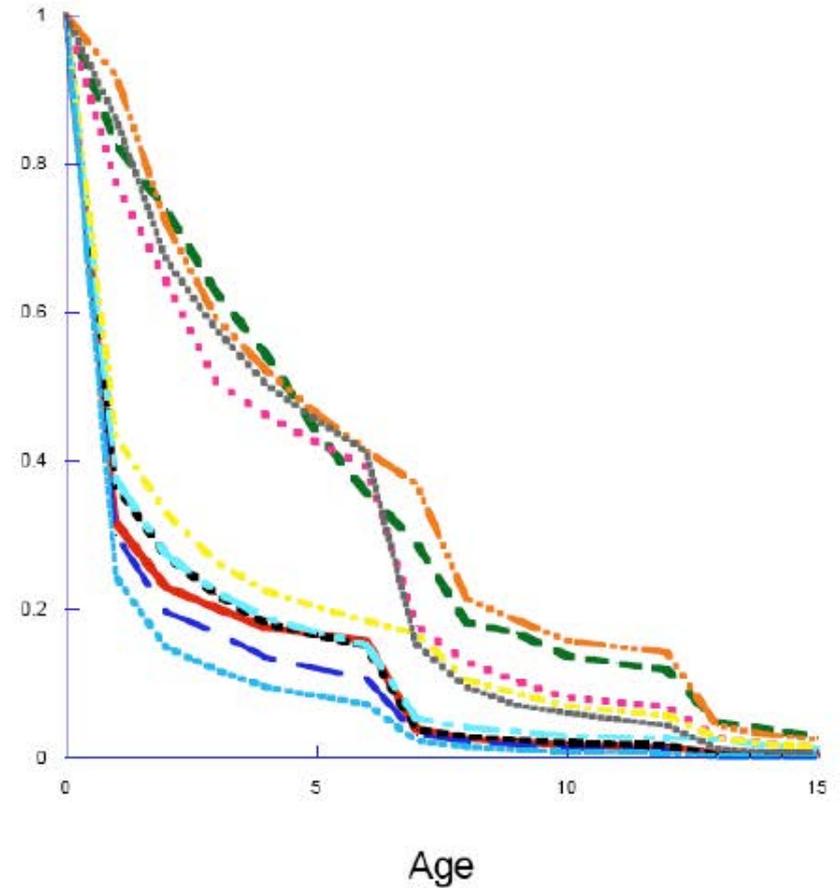
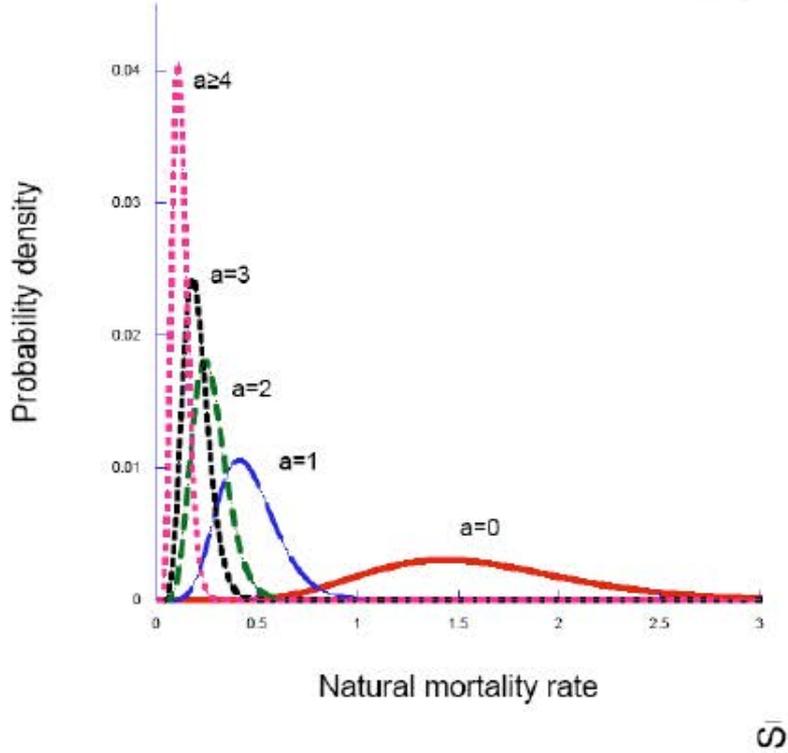
$$\alpha_S(k) = \frac{\sum_n S(A_{n,k}) F(W(A_{n,k})) \cdot n_B}{\sum_n W(A_{n,k})}$$

$$CV(\theta) = 10\%$$

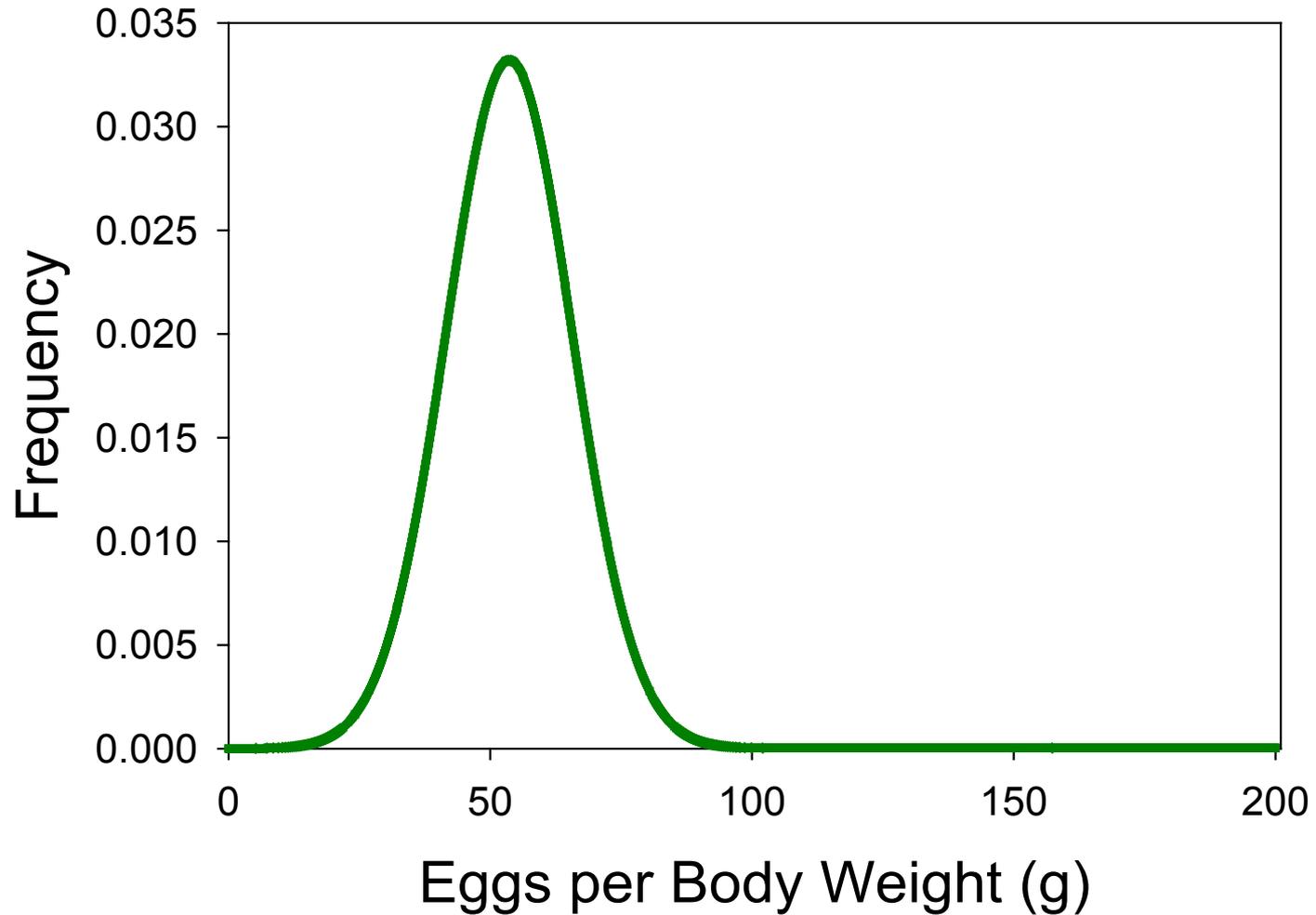
# Striped Marlin Adult Natural Mortality



# Survival Trajectories With Uncertainty in Age Dependent Mortality

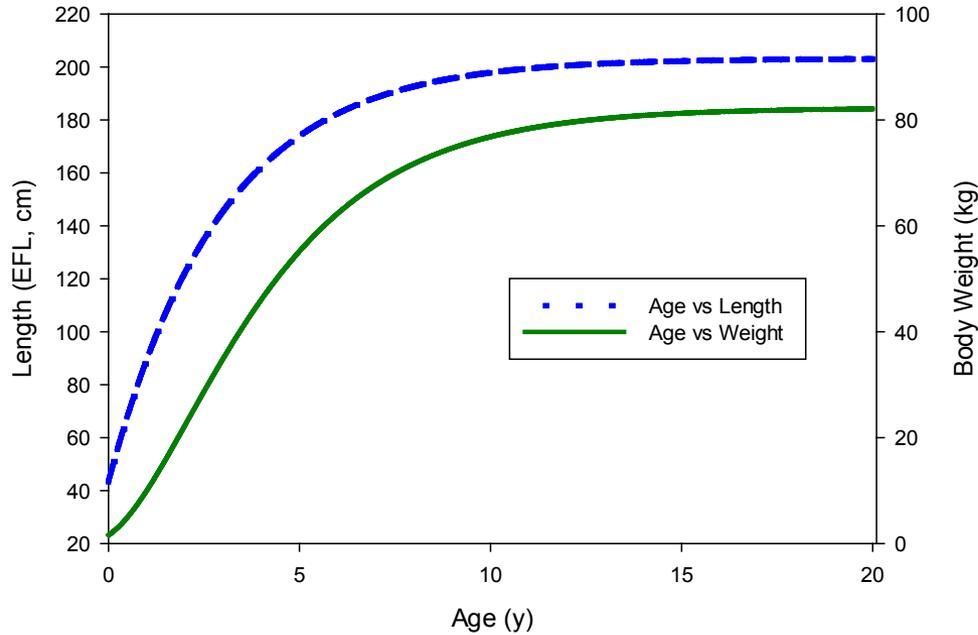


# Striped Marlin Relative Fecundity

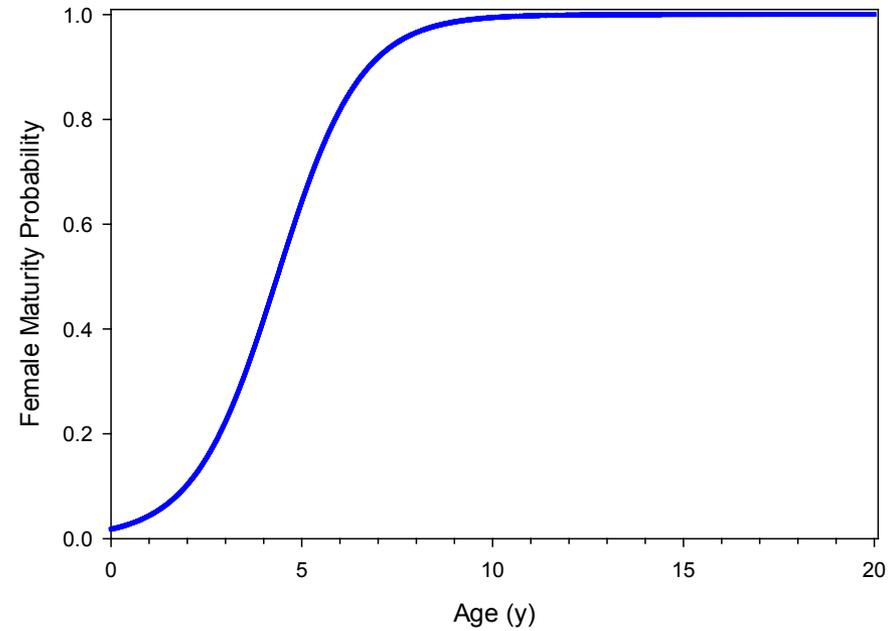


# Striped Marlin Life History Parameters: Adult Size and Maturity at Age

Size at Age



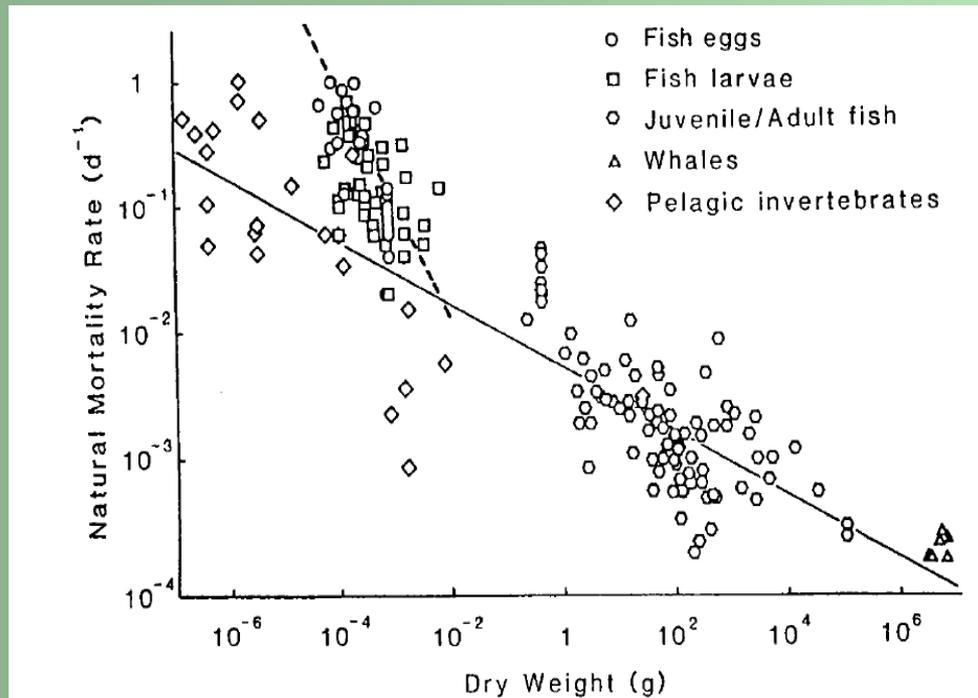
Maturity Ogive



# Modeling Steepness

## Binding Limitations

- Estimation Using Life History Parameters
- Larval Survival  $S_l(d) = S_l(d-1) \cdot \exp(-M_l(w_d))$



$$\frac{\partial \beta}{\partial t} + W \frac{\partial (\beta W)}{\partial t} + \beta M = 0$$

McGurk, M.D. 1986. Natural mortality of marine pelagic fish eggs and larvae: the role of spatial patchiness. *Marine Ecology Progress Series* 34:227-242

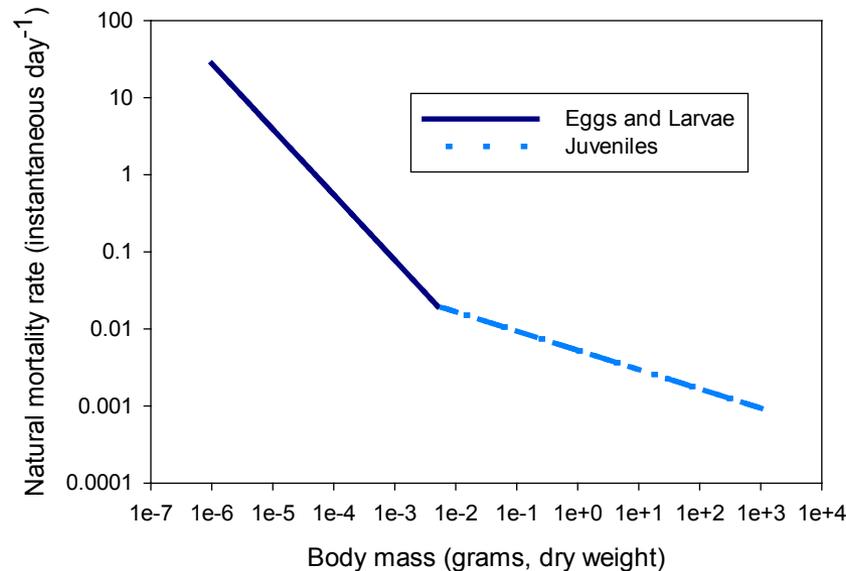
# Early Life History Stage Survival and Growth

## ELH weight (W) by day (d)

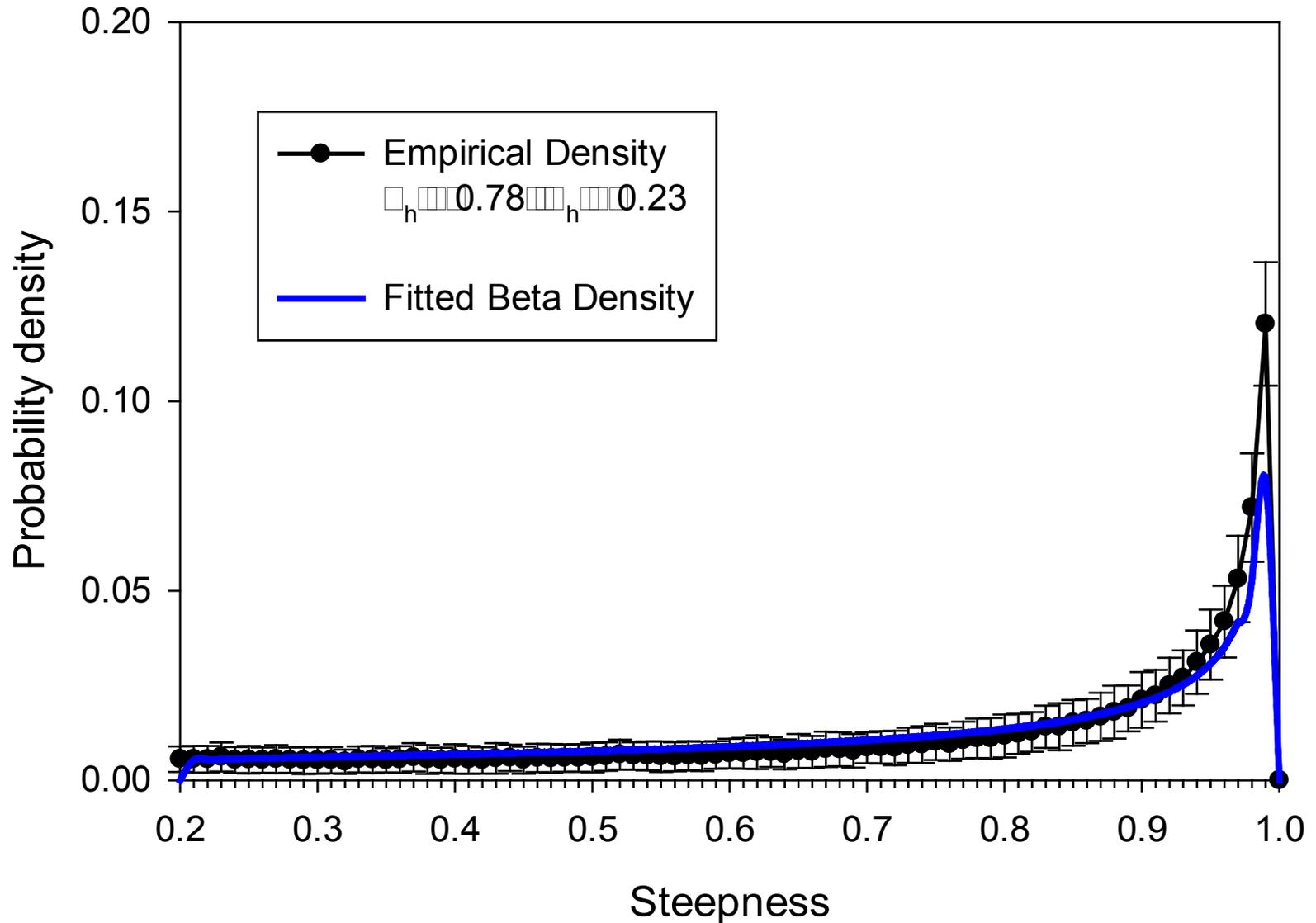
$$W_{ELH}(d) = W_{Egg} \cdot \exp(k_{ELH} \cdot d)$$

## ELH survival (S) to day (d)

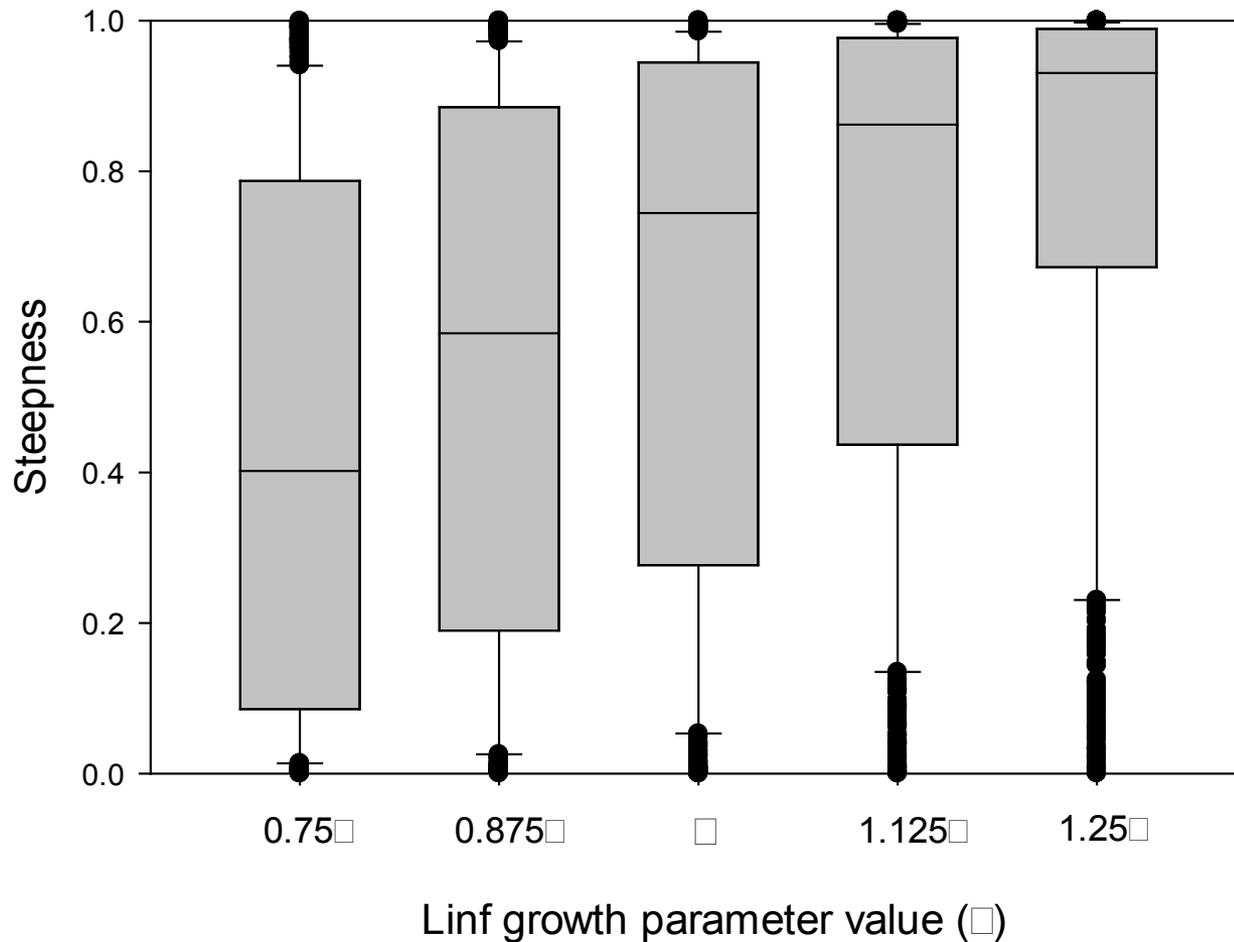
$$S_{ELH}(d) = S_{ELH}(d-1) \cdot \exp(-M(W_{ELH}(d)))$$



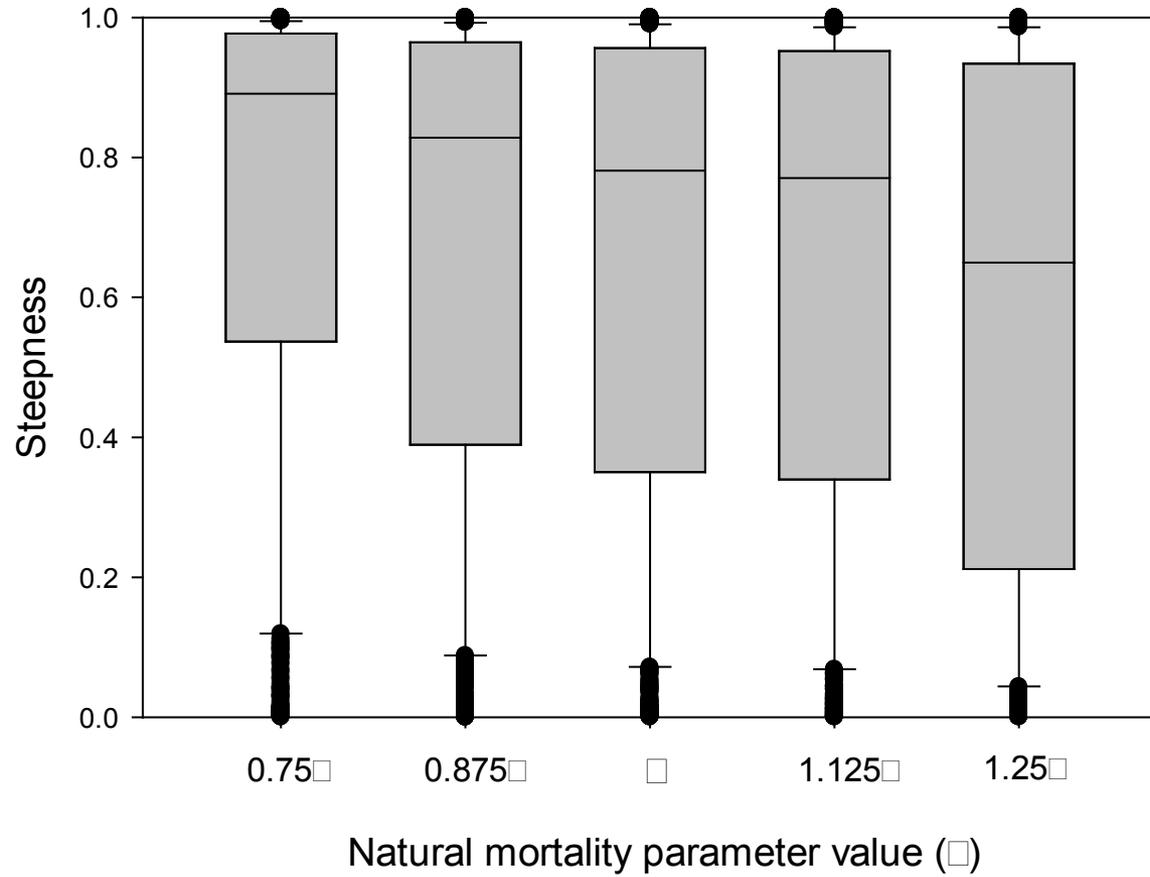
# Striped Marlin Steepness Distribution



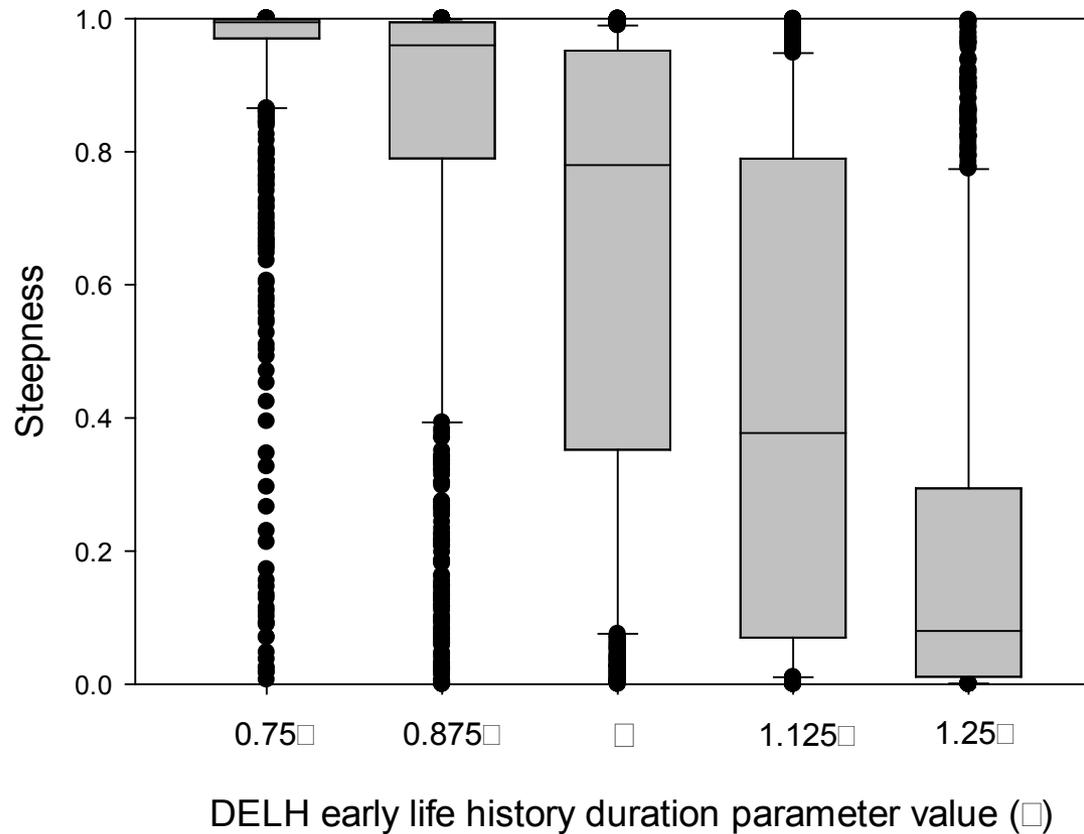
# Sensitivity of Steepness to Asymptotic Length



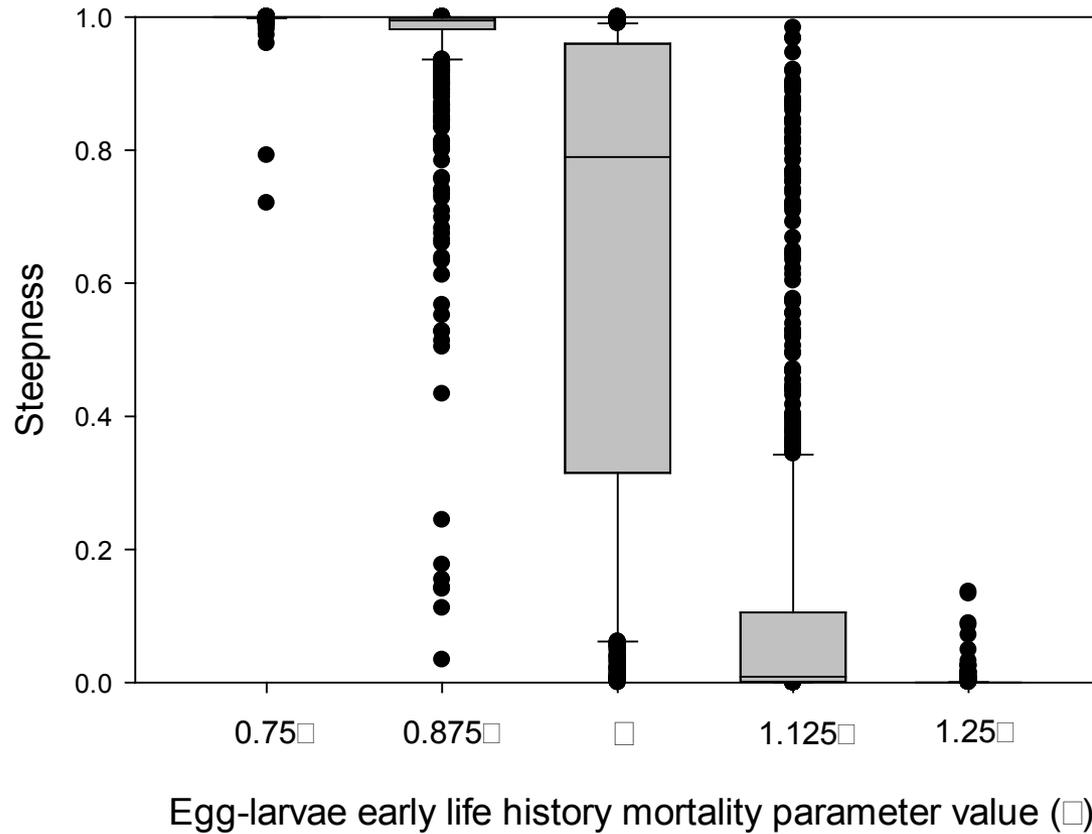
# Sensitivity of Steepness to Adult Natural Mortality Rate (M)



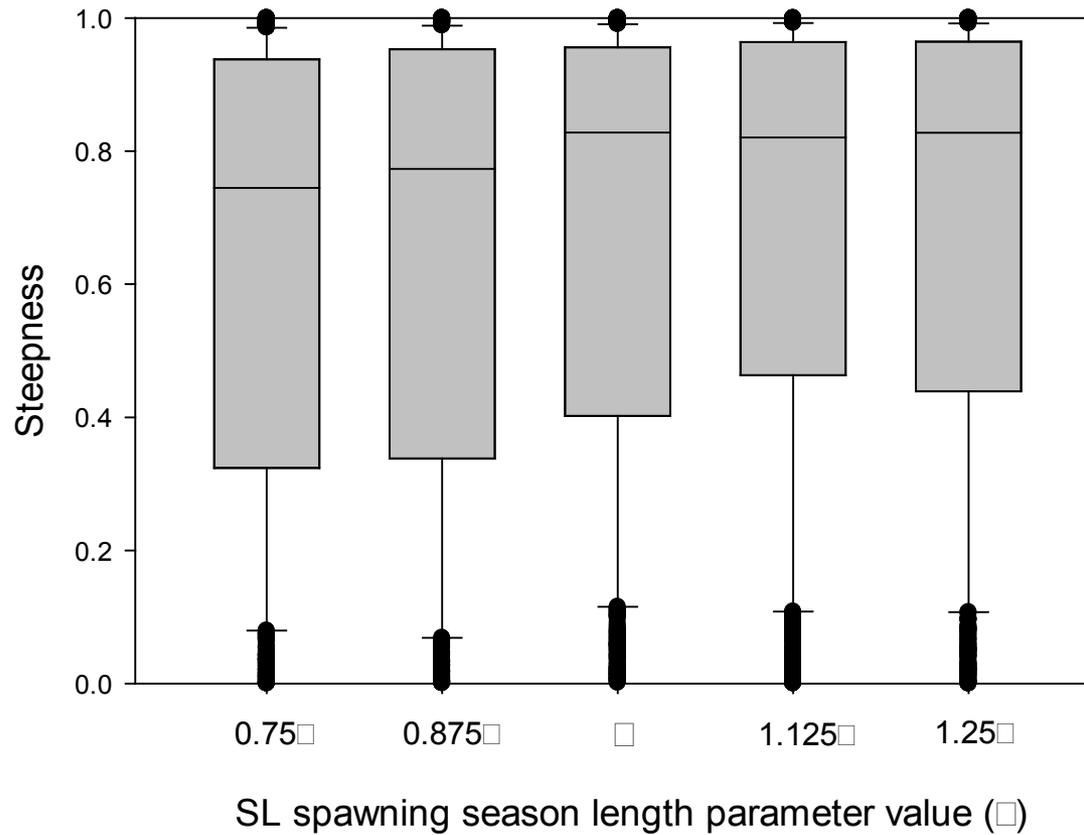
# Sensitivity of Steepness to Early Life History Stage Duration



# Sensitivity of Steepness to Egg-Larval Mortality Slope



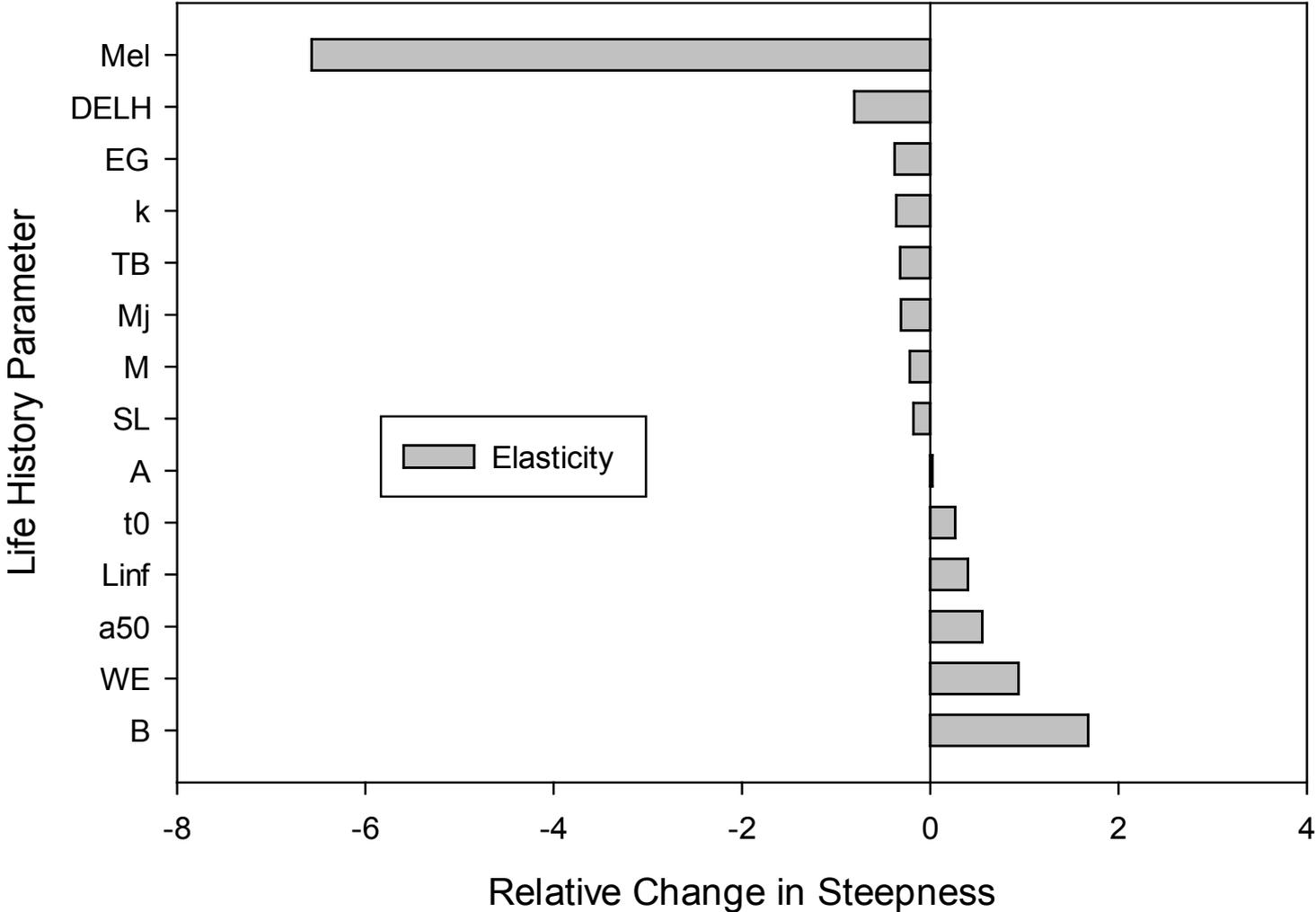
# Sensitivity of Steepness to Spawning Season Duration



# Characterizing Parameter Sensitivity: Elasticity of Steepness ( $h$ ) to Parameters $\theta_k$

$$U_h(\theta_k) = \frac{\partial h}{\partial \theta_k}(\underline{\theta}) \cdot \left( \frac{h}{\theta_k} \right)^{-1}$$

# Comparing Elasticities of Life History Parameters

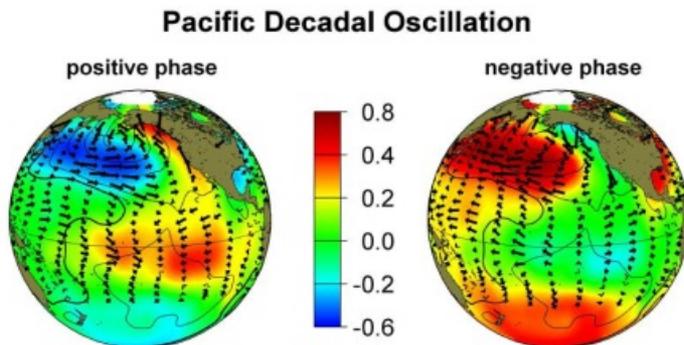


# Conclusions and Future Research

- Given an age-structured model for cohort dynamics with stochastic variation, one can determine an associated distribution of steepness  $h$
- As a result, choosing an arbitrary steepness value will produce model misspecification in an assessment

# Conclusions and Future Research

- Striped marlin steepness is likely relatively high, but has a broad range of uncertainty that should be reflected in the stock assessment
- Steepness is sensitive to reproductive ecology and more work is needed:
  - ✓ Extend standard model with environmental linkage
  - ✓ Focus on ELH data collection and metaanalysis
  - ✓ Create world-wide ELH information database



Thanks and Mahalo ~!

