




# **The performance of a Z-level coordinate model in modeling global tide**

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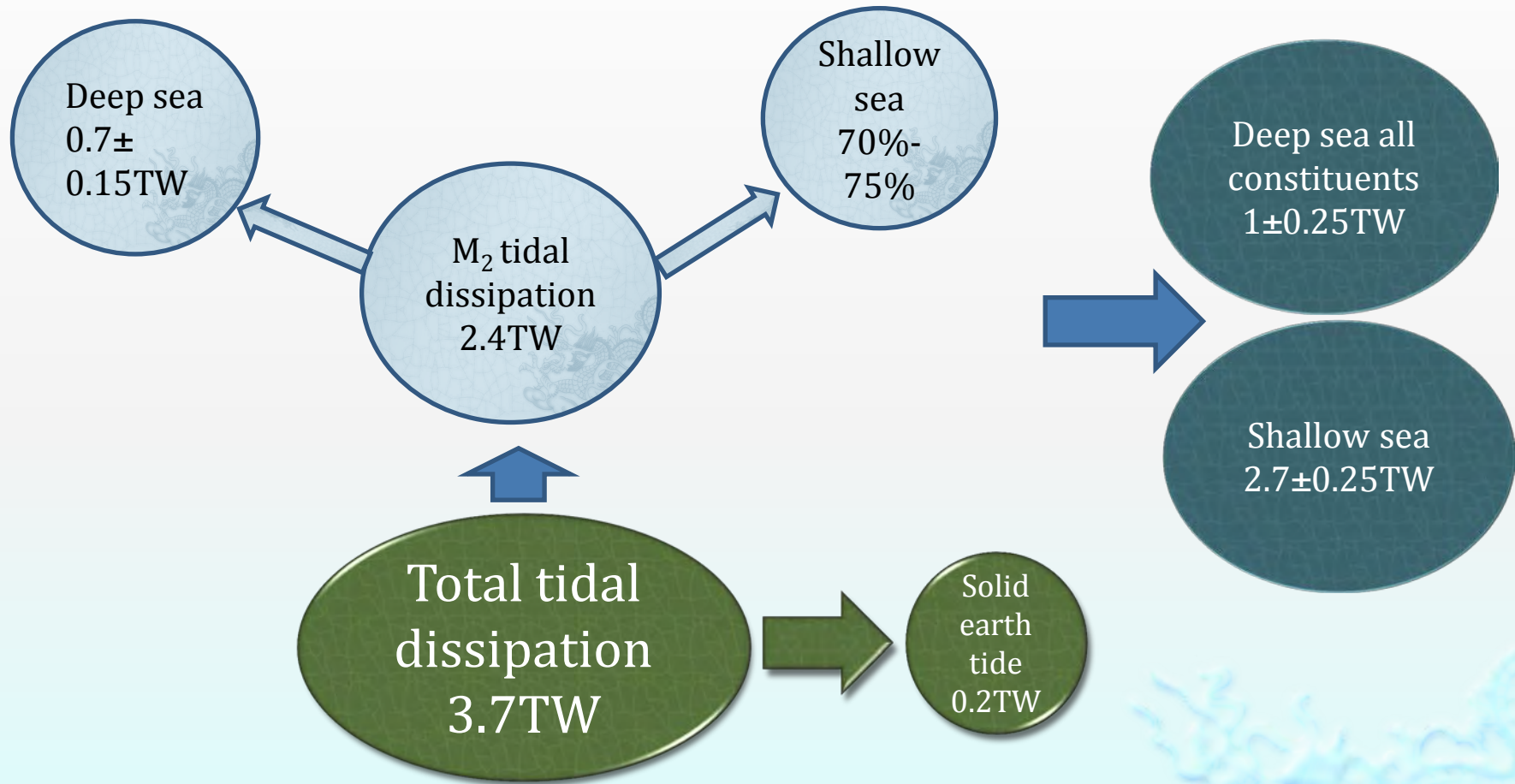
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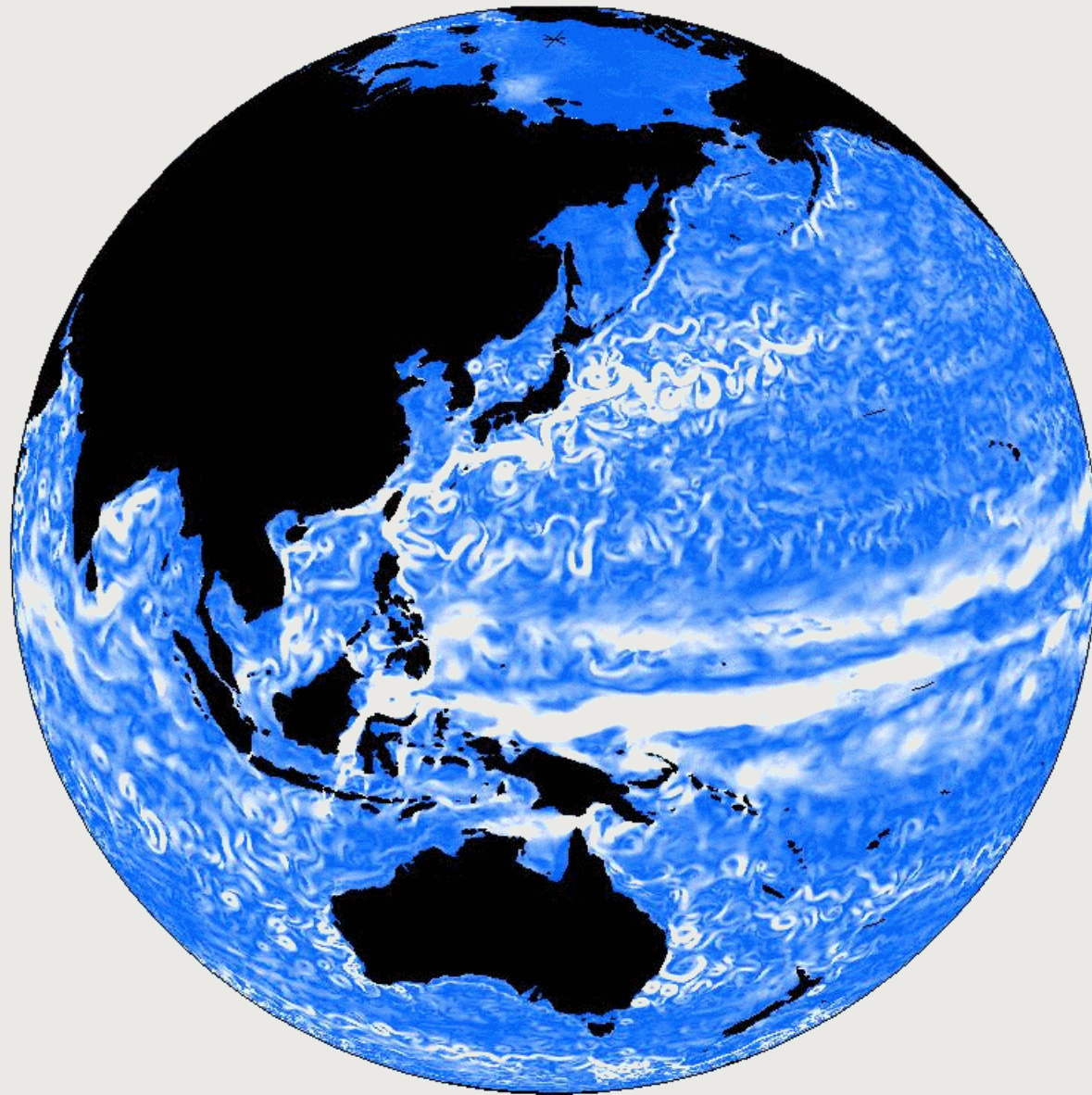
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# 1. Motivation and research background



(Egbert and Ray, 2000)





**Could we set up high-resolution wave-tide-circulation coupled model?**

# 1. Motivation and research background

## **First type global tide model is based on barotropic laplacian tidal equation**

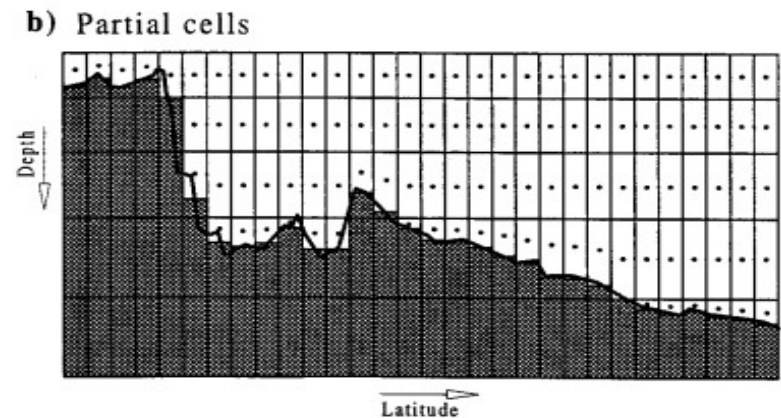
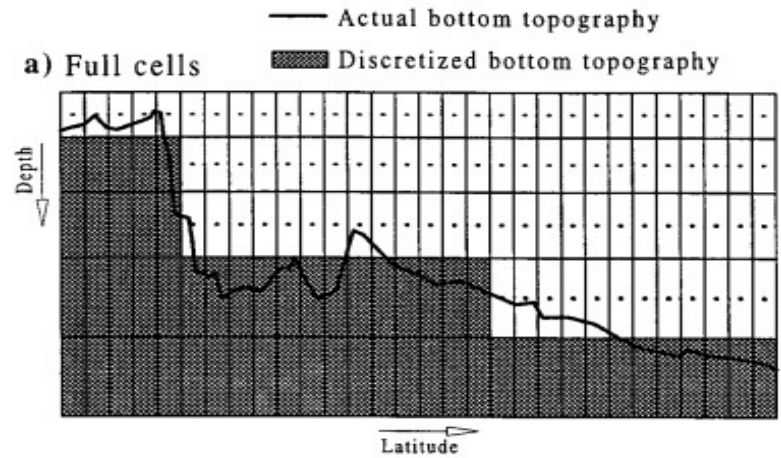
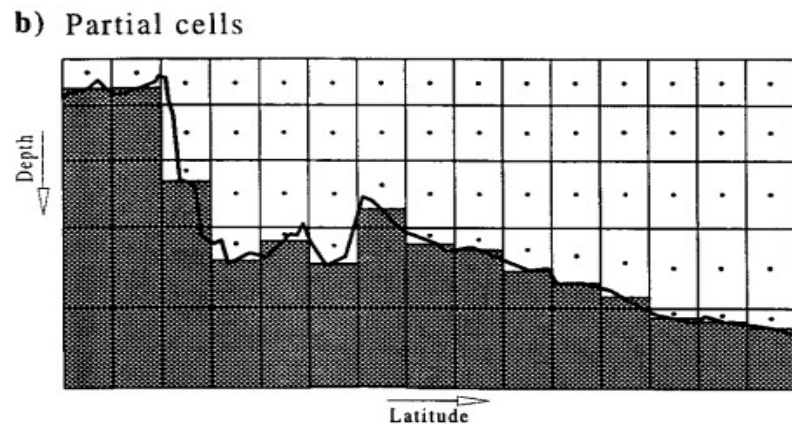
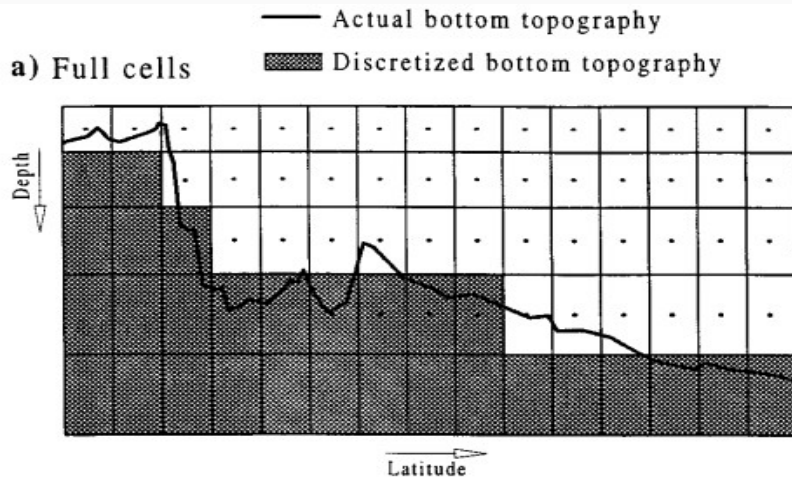
- ◆ JS model: Barotropic global tide model, internal tide drag parameterization ;  
(Jayne and St. Laurent , 2001)
- ◆ ERB model : Barotropic global tide model, internal tide drag parameterization, complete self-attraction and loading (SAL) treatment;  
(Egbert et al. 2004)

## **Second type puts the equilibrium tidal potential into the OGCM(baroclinic)**

- ◆ SHA model: HIM, 10 vertical layers, horizontal resolution:  $1/8^\circ$ , Self-Attraction and Loading effect(SAL) is scalar approximation;  
(Simmons et al. 2004)
- ◆ AGHS model : HIM, HYCOM, internal tide drag parameterization, horizontal resolution:  $1/2^\circ$  to  $1/12.5^\circ$ , SAL is scalar approximation.  
(Arbic et al. 2004, 2010)

# 1.1 Modular Ocean Model (MOM4)

## Bottom partial cells



Comparison between Full cells and Partial cells under the same vertical resolution and different horizontal resolutions (Pacanowski and Gnanadesikan, 1998)



# 1.2 Inclusion of tidal forcing in MOM4 (Marchuk and Kagan, 1989)

- ◆ Equilibrium tidal potential :

$$\text{and } \eta_n(t) = H_n \sin 2\phi \cos(\omega_n t + \chi_n + \lambda)$$

$$\eta_n(t) = H_n \cos^2 \phi \cos(\omega_n t + \chi_n + 2\lambda)$$



$$\eta_{eq} = \sum_{n=1}^4 [\beta_n \alpha_n \cos^2 \phi [\cos(\omega_n t) \cos 2\lambda - \sin(\omega_n t) \sin 2\lambda] + \beta_{n+4} \alpha_{n+4} \sin 2\phi [\cos(\omega_{n+4} t) \cos 2\lambda - \sin(\omega_{n+4} t) \sin 2\lambda]]$$



$$\partial \mathbf{U} / \partial t = -f \mathbf{k} \times \mathbf{U} - D \nabla_h [\alpha p_s / \rho_0 - \beta g \eta_{eq}] + G - \tau_{tides} / \rho_0$$

Beta represents LOVE number, accounting for the reduction of the ocean tide because of the deformation of the solid earth by tidal forces.

$$\tau_{tides} = \rho_0 c_d |\mathbf{u}| \mathbf{u}$$

$$c_d \approx 0.0025$$

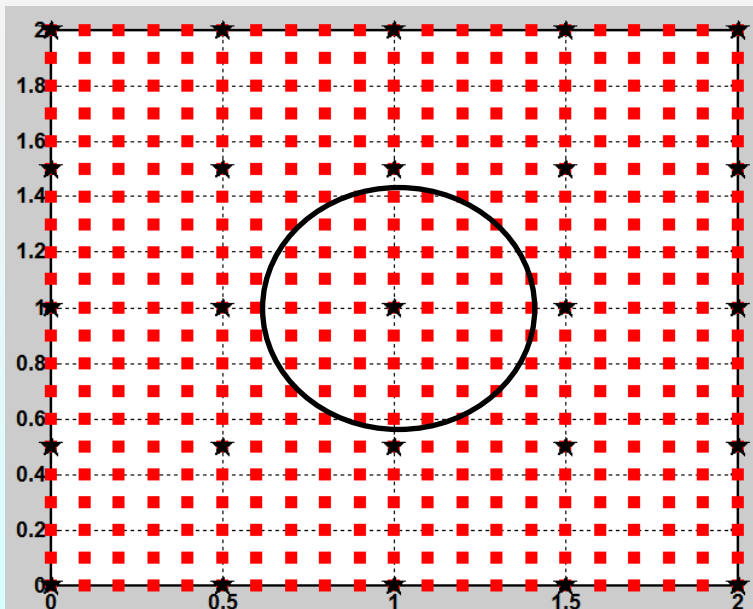
## 2. Influence of model topography on global tide

### 2.1 Preparation of model topography

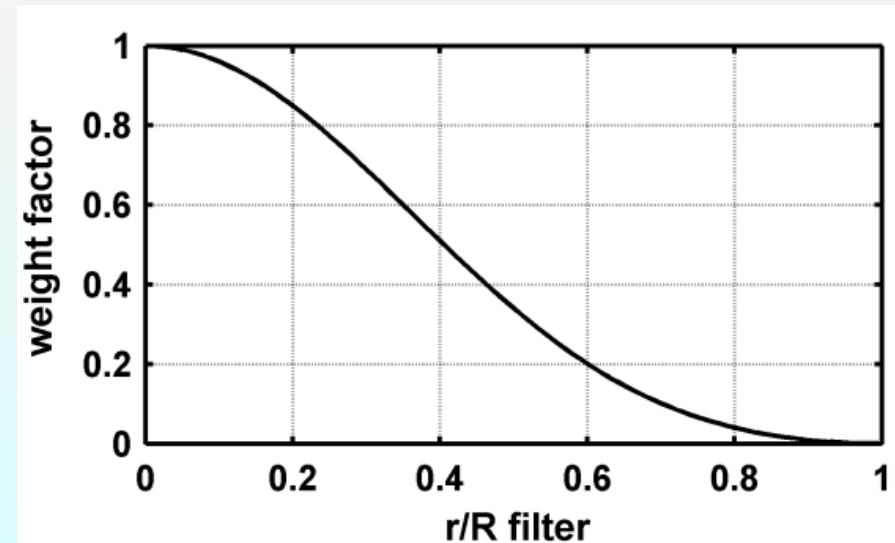
- ◆ Blackman radial filter (Arbic et al. 2004) :

$$\text{Filted}(x, y) = \frac{\iint \text{src}_{\text{fine\_grid}}(x', y') F(x, y, x', y') dA}{\iint F(x, y, x', y') dA}$$

$$F(x, y, x', y') = 0.42 + 0.5 \cos(\pi r_{\text{field}} / r_{\text{filter}}) + 0.08 \cos(2\pi r_{\text{field}} / r_{\text{filter}})$$



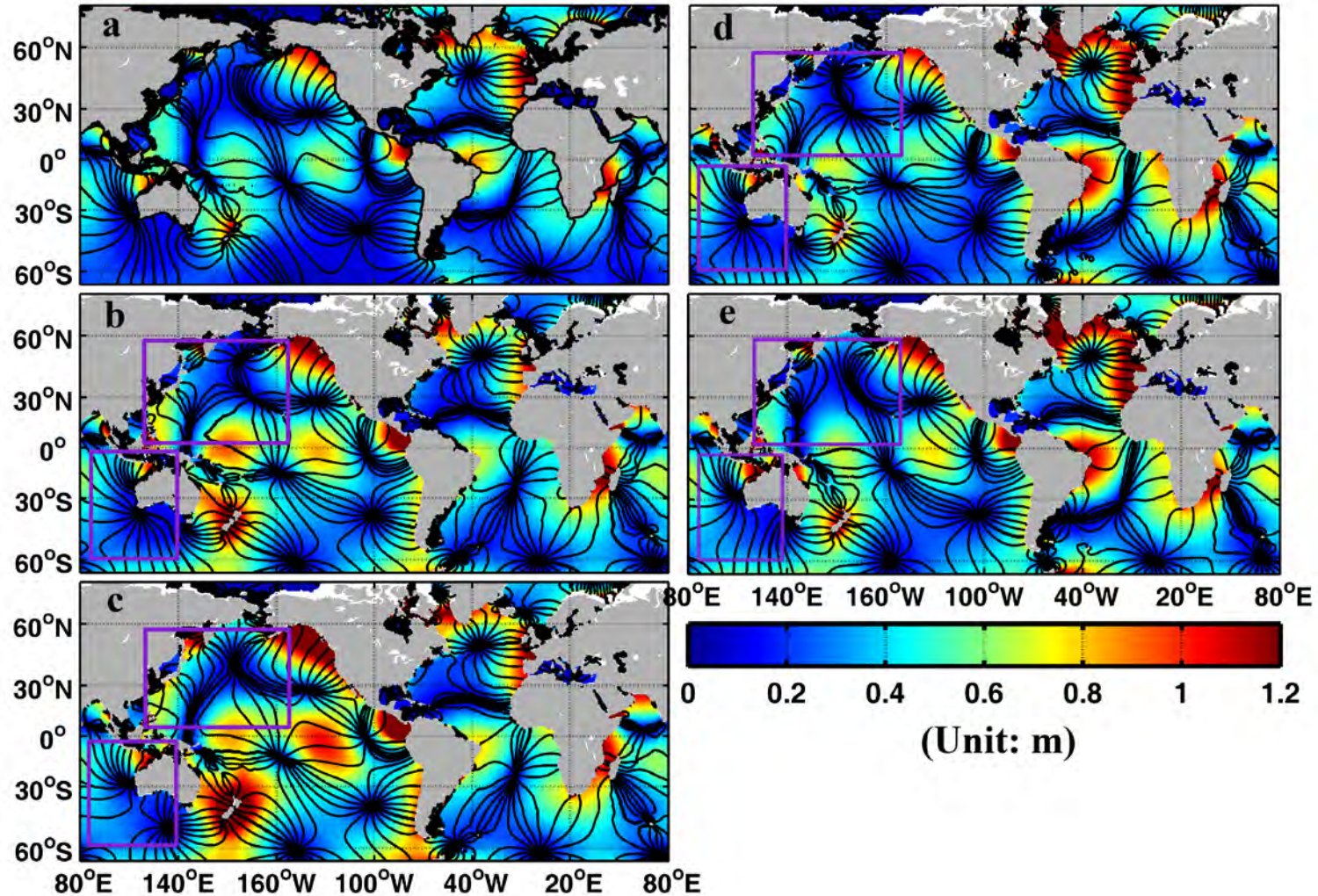
Schematic diagram of radial filter



Weight factor of Blackman radial filter

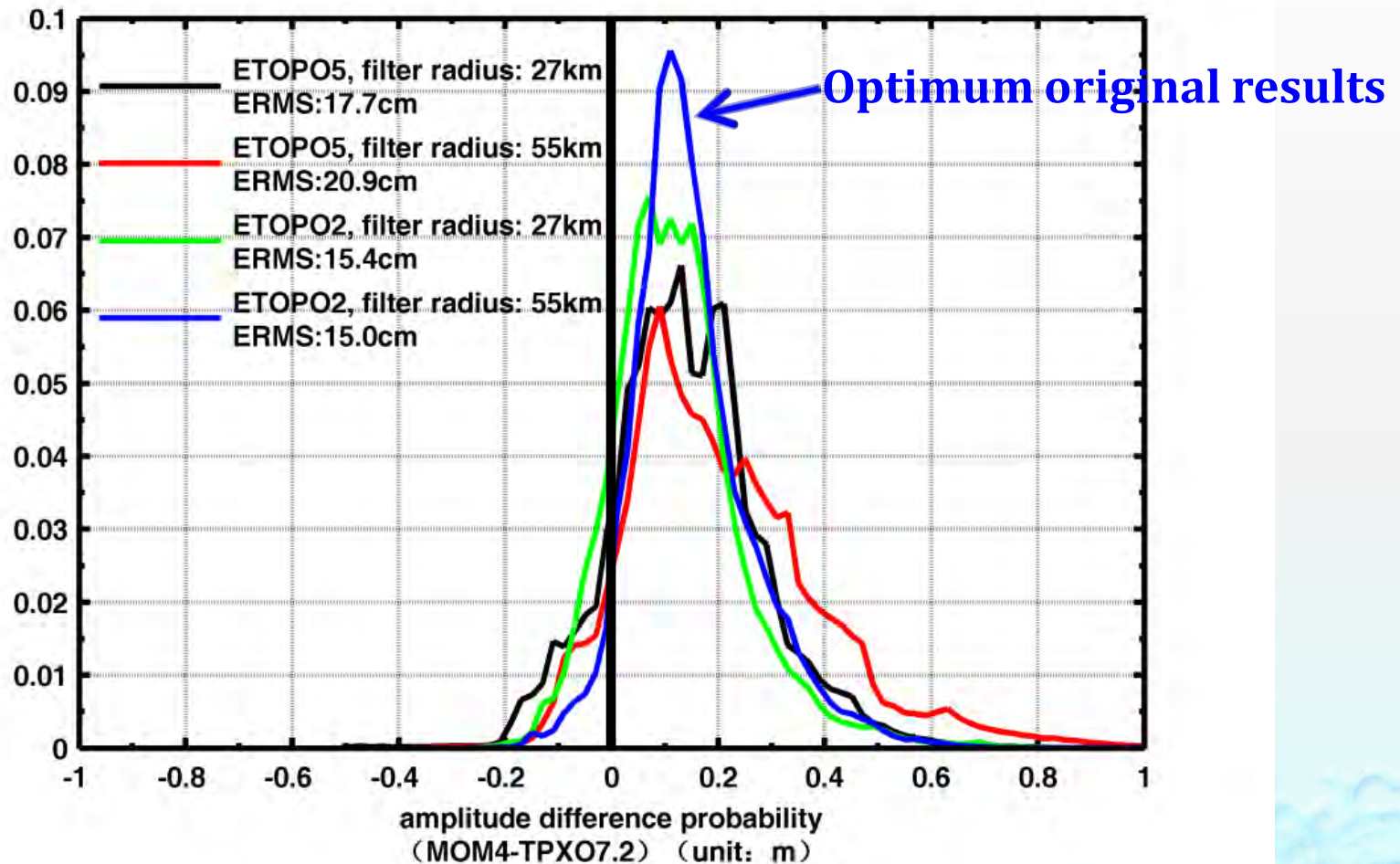


## 2.2 Model topography sensitive experiments



Amplitude and phase (contour interval: 20°) of , (a) is from TPX07.2, (b) is result of MOM4 (1/4°) and model topography is built from ETOP05 with filter radius 27km. (c) (d) (e) are identical to (b) except that the model topography of (c) is built from ETOP05 with filter radius 54km, (d) is built from ETOP02 with filter radius 27km, (e) is built from ETOP02 with filter radius 54km.

## 2.2 Model topography sensitive experiments

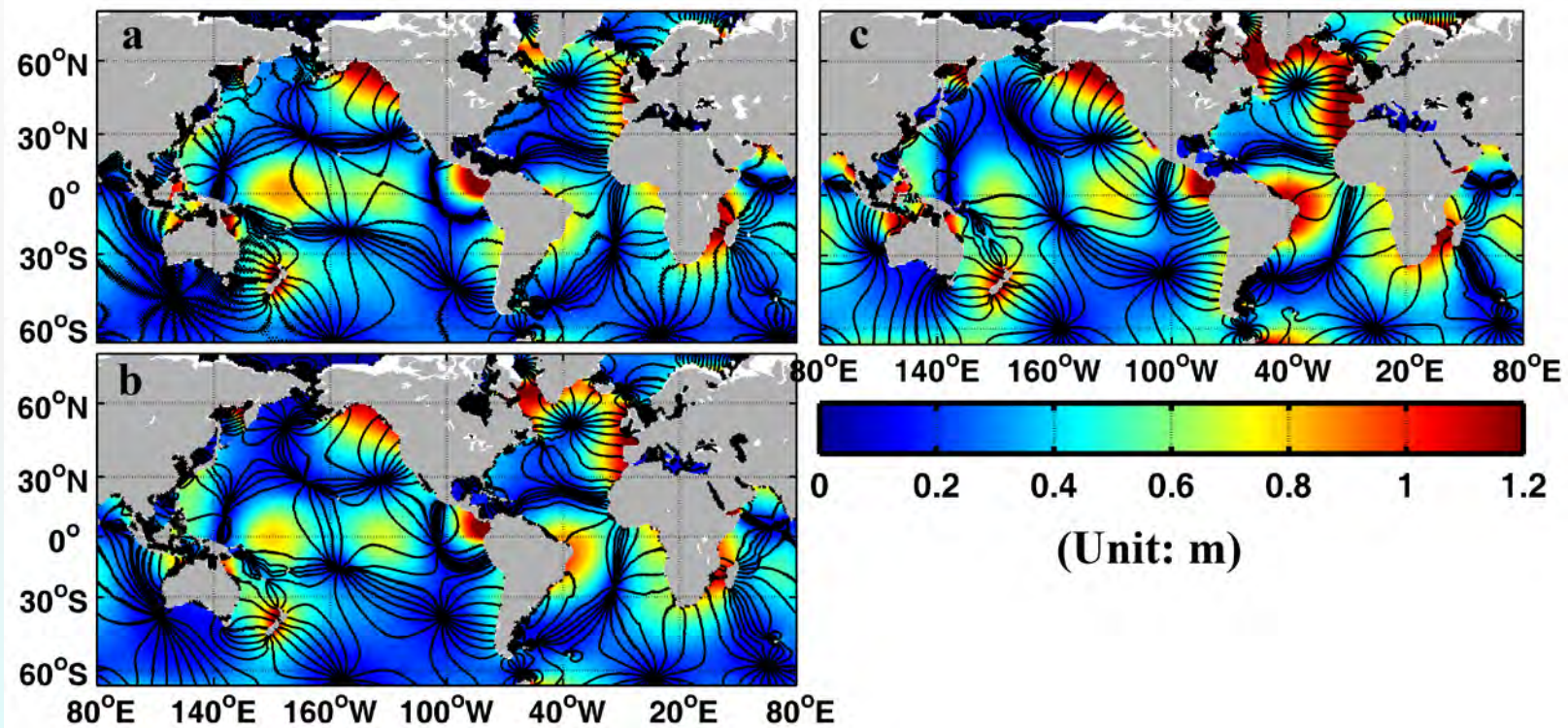


$M_2$  amplitude difference probability distribution between MOM4 and TPX07.2 in corresponding to the 4 sensitive experiments.



# 3, Critical model resolution

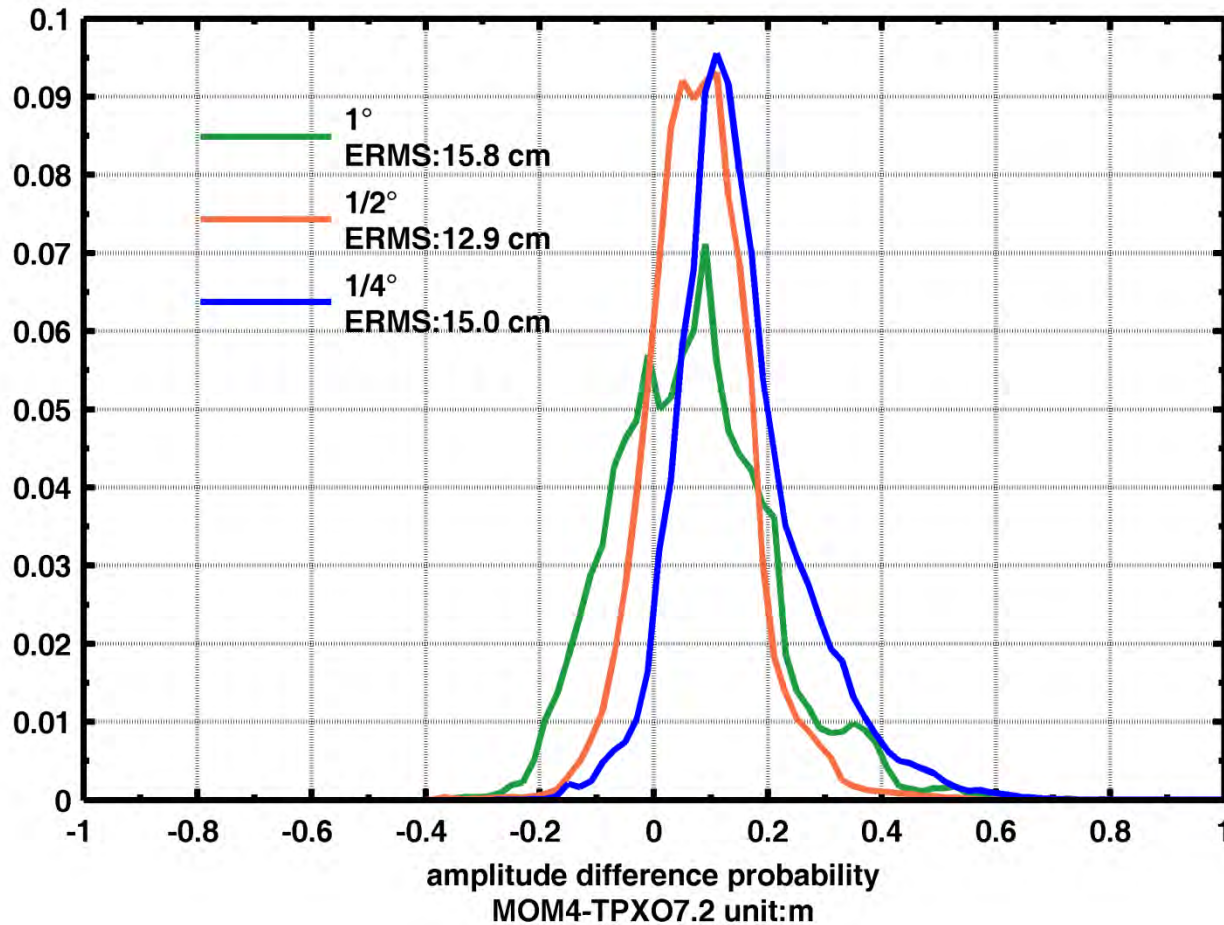
## 3.1 Horizontal resolution



(a) 1° model results, (b) 1/2° model results, (c) 1/4° model results

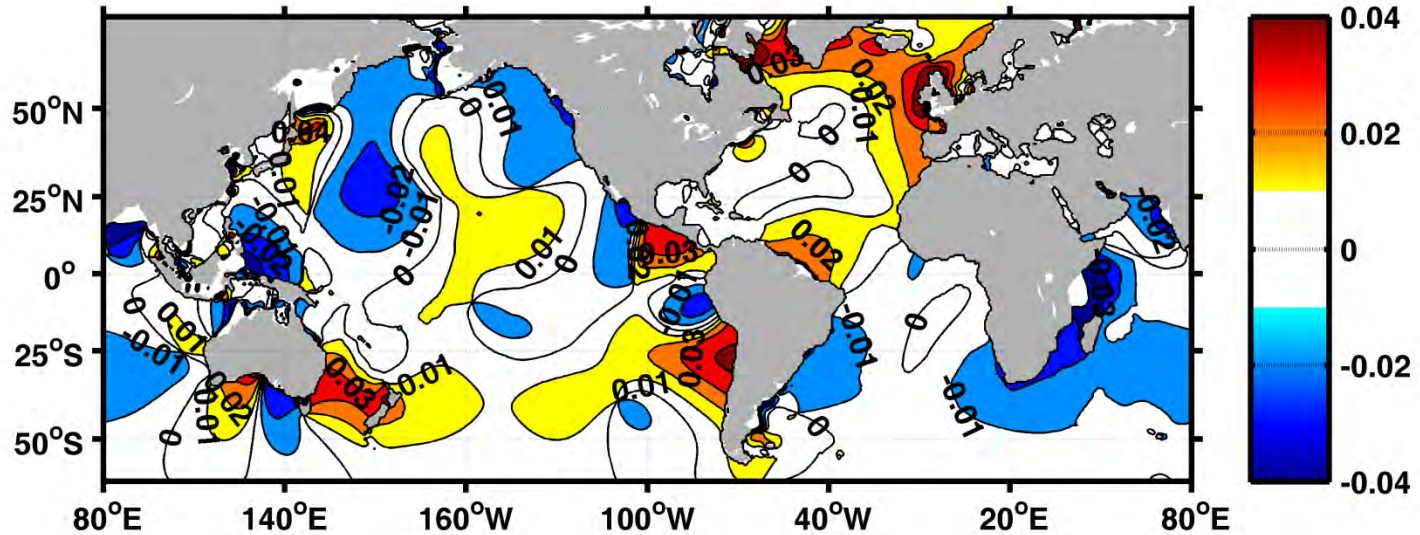


## 3.1 Horizontal resolution



$M_2$  amplitude difference probability distribution between MOM4 and TPX07.2 in corresponding to the 3 sensitive experiments.

## 3.2 Vertical resolution



$M_2$  amplitude difference between 11 levels model and 34 levels model (horizontal resolution  $1/4^\circ$ , 11 levels minus 34 levels model).

**RMS difference is 1.2cm**

## 4. Inclusion of internal tide dissipation parameterization

### 4.1 Parameterize the internal tide dissipation

- ◆ Bell (1975) proposed a theory on energy conversion between barotropic and baroclinic tide based on the assumption of small amplitude sinusoidal topography :

$$E_f = \frac{(\omega^2 - f^2)^{1/2}}{2\omega} \rho_0 \kappa h^2 Nu^2$$

- ◆ Jayne and St. Laurent (2001) simplified Bell's theory by ignoring the tidal frequency related terms and by replacing the h with topography roughness and come up with :

$$E_f = \frac{1}{2} \rho_0 \kappa h^2 Nu^2$$

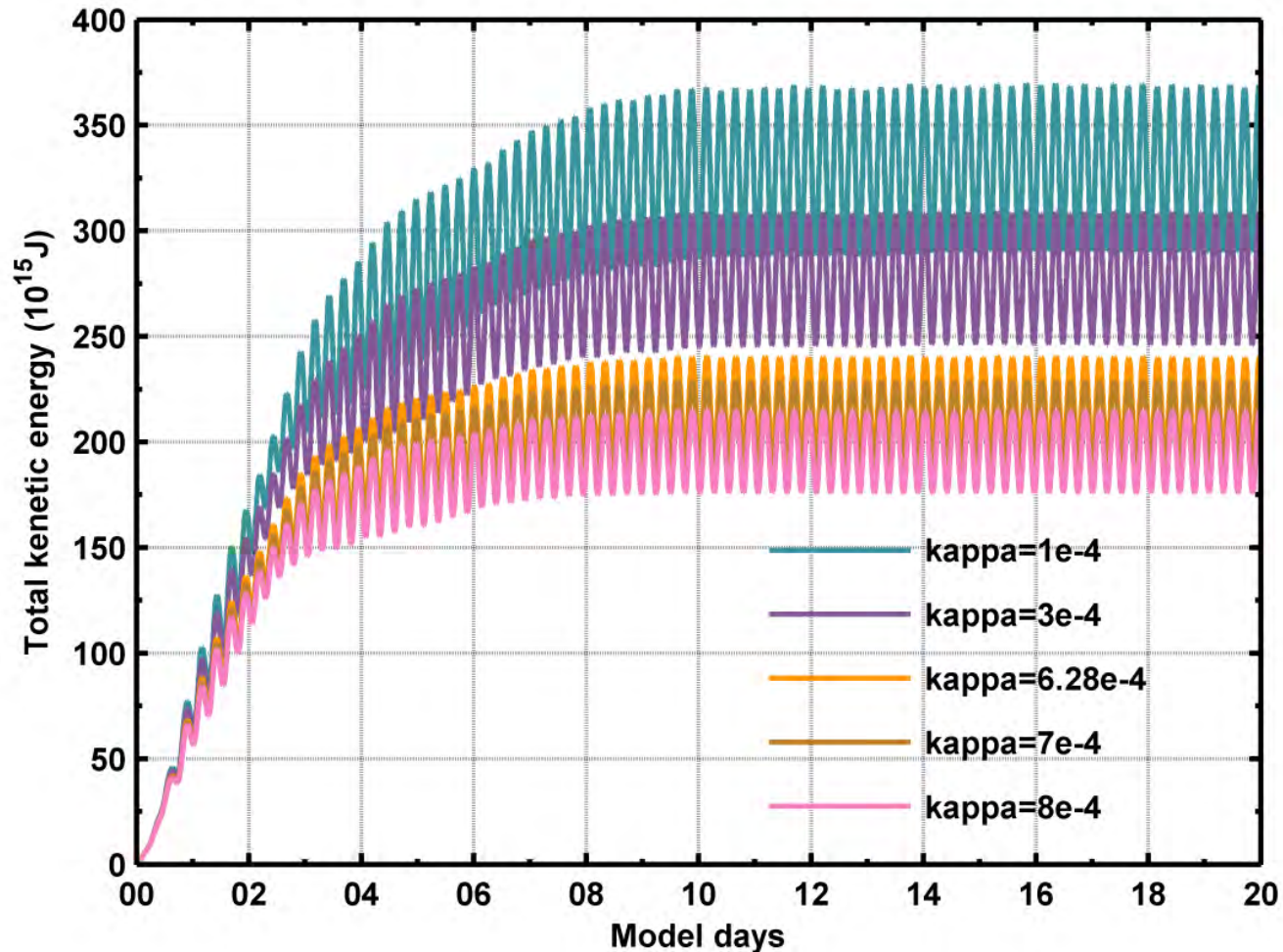
- ◆ We add the above parameterization (IT drag) into the barotropic momentum equation :

$$\partial \mathbf{U} / \partial t = -f \mathbf{k} \times \mathbf{U} - D \nabla_h [\alpha p_s / \rho_0 - \beta g \eta_0] + G - \tau_{tides} / \rho_0 - \frac{1}{2} \kappa h^2 Nu$$



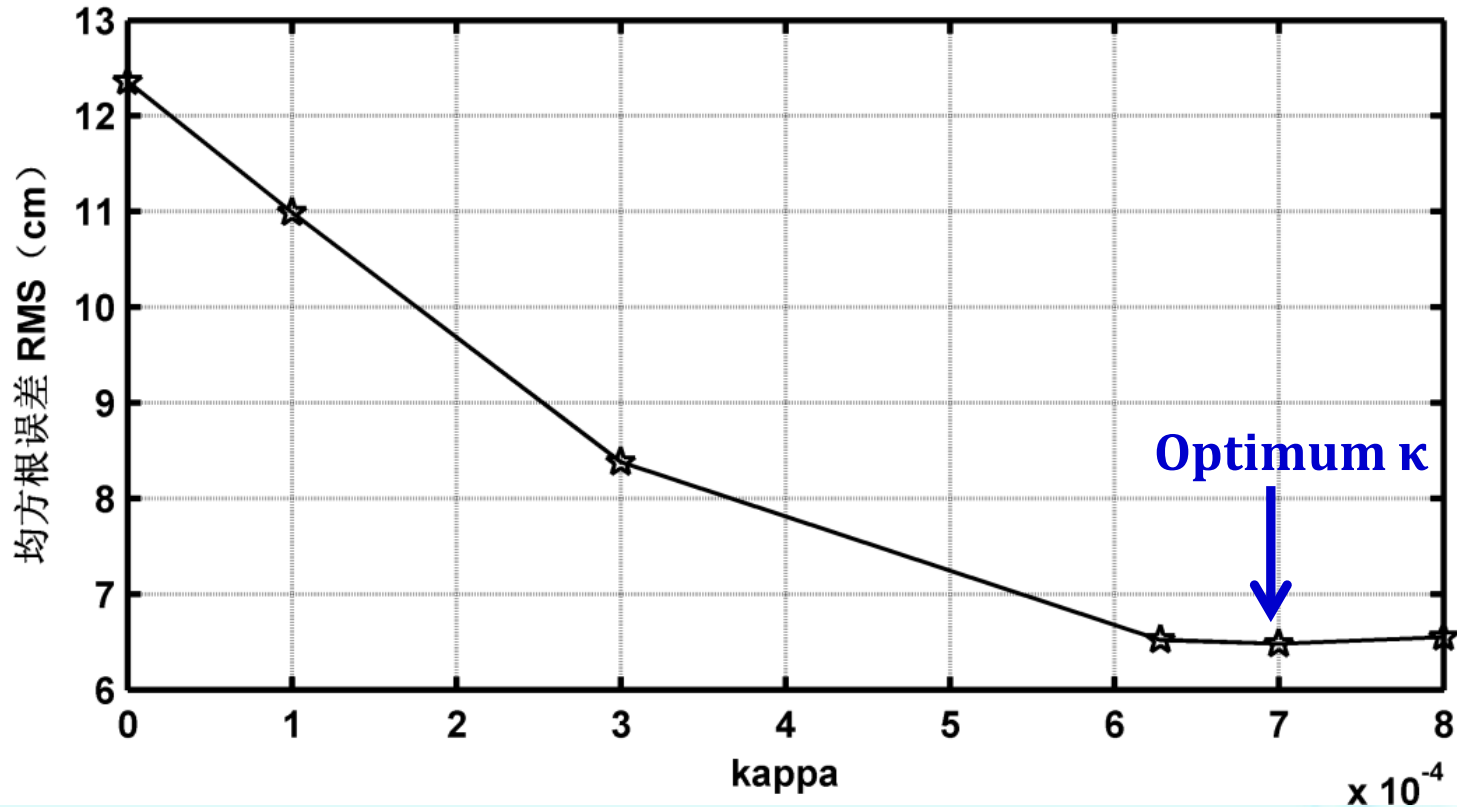
## 4.2 Model results with inclusion of internal tide drag parameterization

$$\kappa = 1 \times 10^{-4} \rightarrow 8 \times 10^{-4}$$



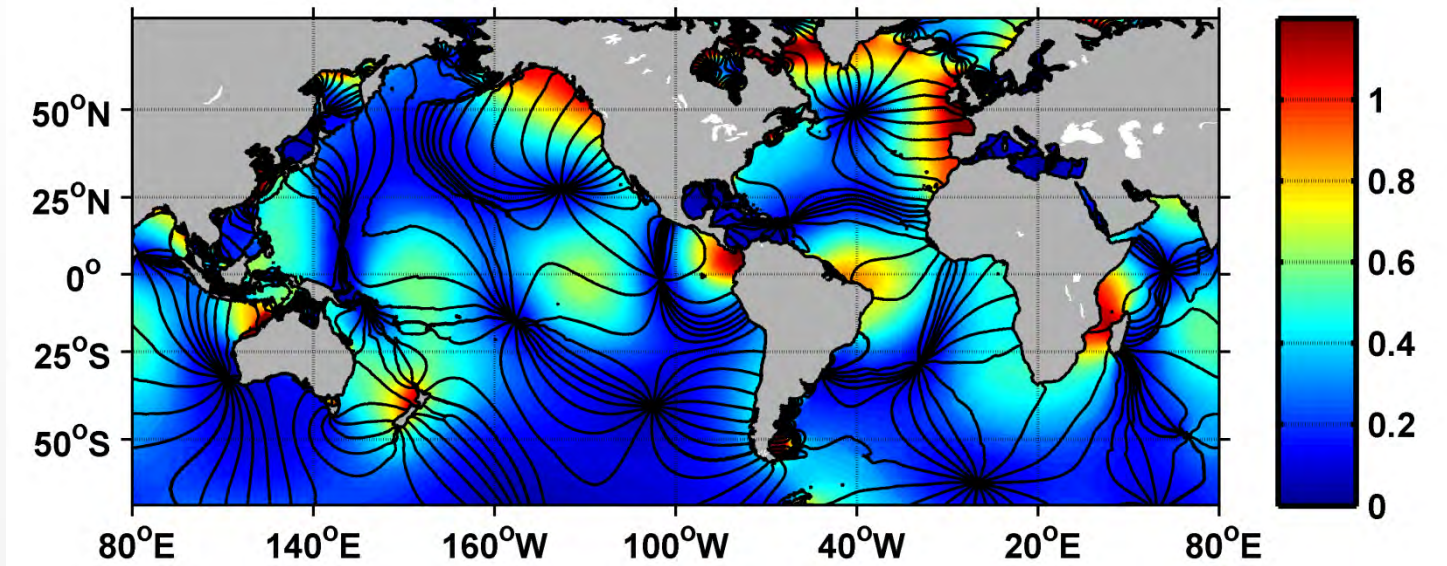
Total kinetic energy under different  $\kappa$  ( $M_2$  only runs)

## 4.2 Model results with inclusion of internal tide drag parameterization

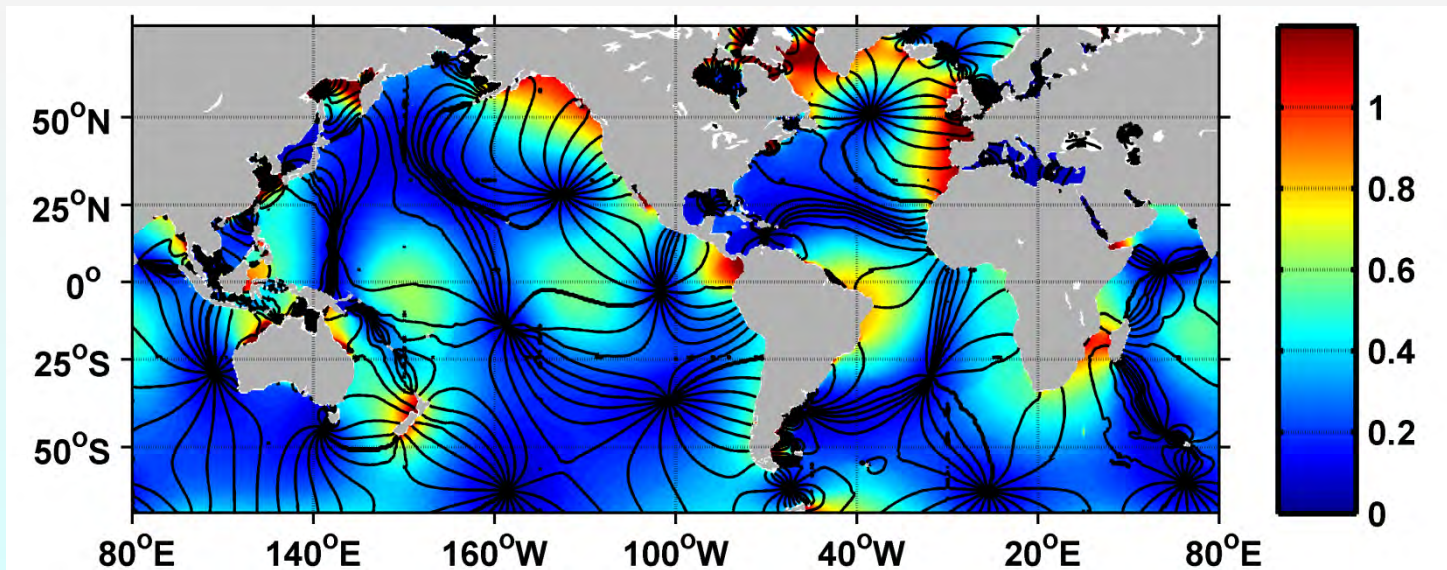


Modeled  $M_2$  amplitude RMS(ARMS) errors compared with TPX07.2 under different  $\kappa$ .



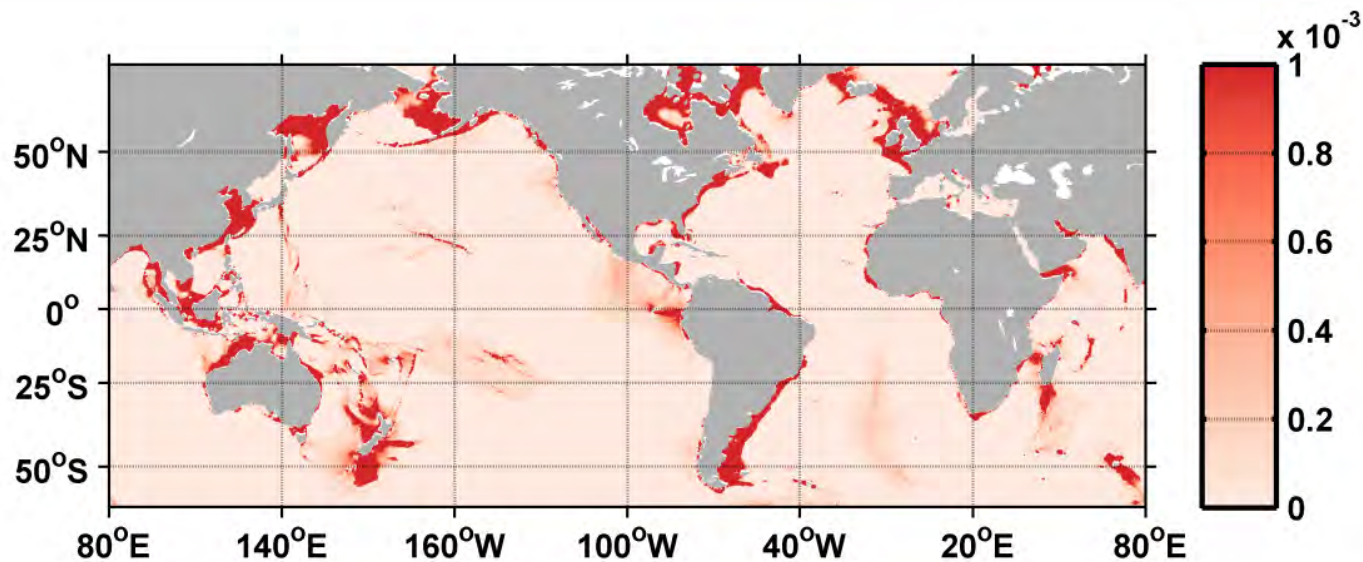


**M<sub>2</sub> co-tidal charts of TPX07.2**



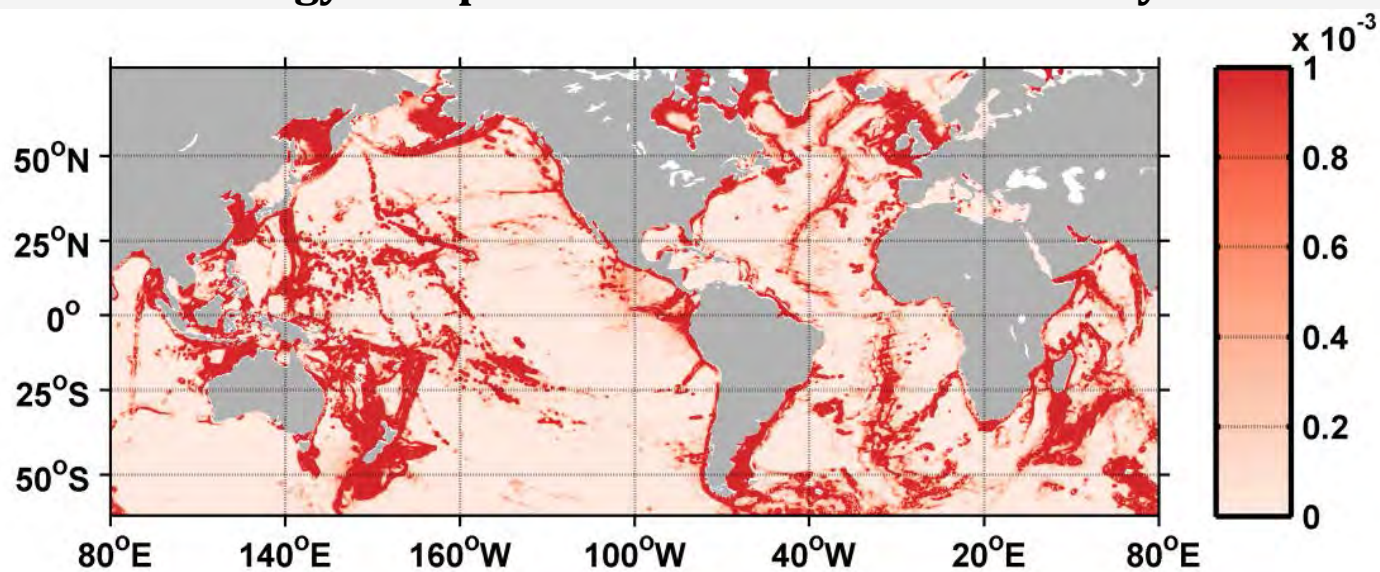
**Modeled M<sub>2</sub> co-tidal charts  $\kappa = 7.0e-4$**





$$c_d \rho_0 \left\langle \left| \vec{u} \right|^3 \right\rangle$$

**Tidal energy dissipation with bottom friction only**  $W/m^2$



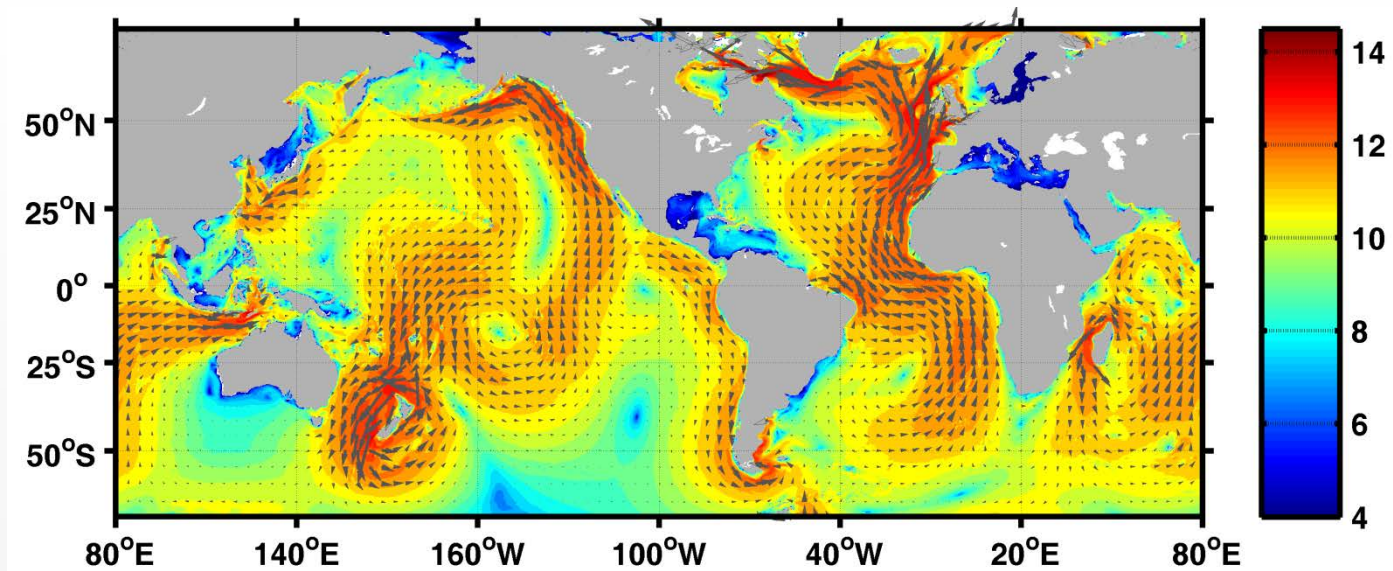
$$c_d \rho_0 \left\langle \left| \vec{u} \right|^3 \right\rangle + \frac{1}{2} \rho_0 \kappa h^2 N \left\langle \left| \vec{u} \right|^2 \right\rangle$$

**Tidal energy dissipation with inclusion of IT drag term**  $W/m^2$

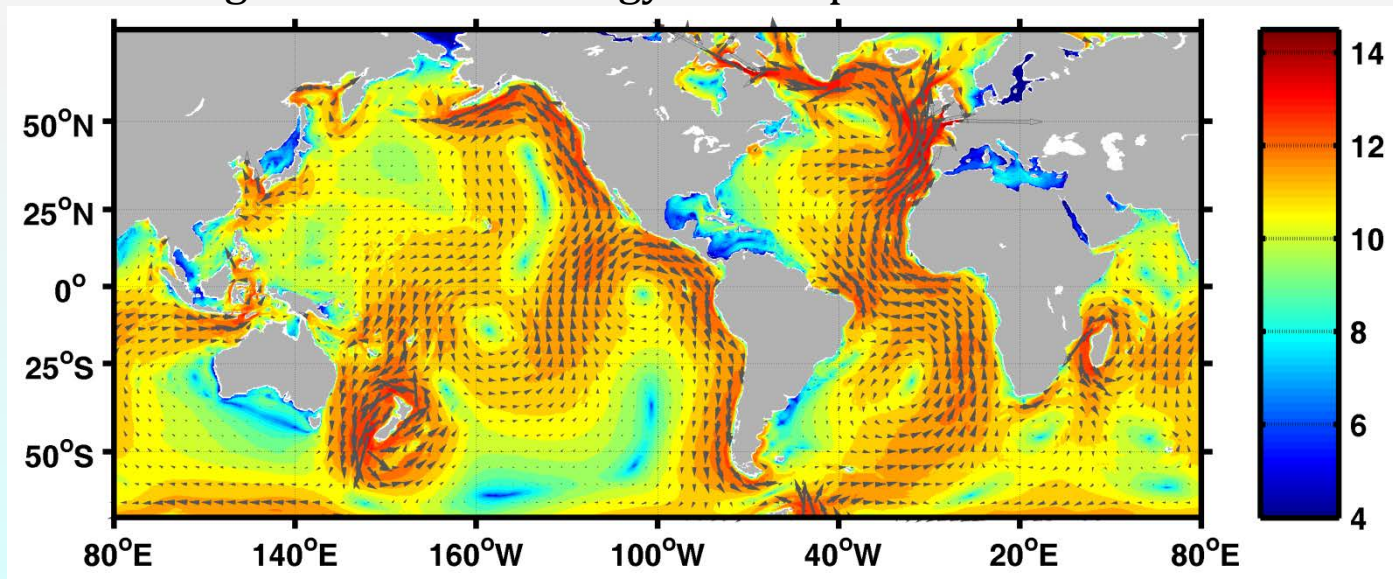
	Jayne, St. Laurent (2001)	Egbert et al. (2004)	Arbic et al. (2004)	Arbic et al. (2012)	Müller et al. (2010)	MOM4
Comparison Datasets	UT-CSR	TPX0.5	ST102	<u>ST102</u>	ST102	TPX07.2
Comparison Area	72°S-72°N, water depth > 1000m	66°S-66°N, water depth > 1000m	77°S-63°N	77°S-63°N	77°S-63°N	66°S-66°N, water depth>1000m
M <sub>2</sub> RMS: cm	ERMS: 6.7	ERMS: ~5.0	ERMS: 9.3	ERMS: 8.3	ARMS: 12.	ERMS/ARMS: 8.5/6.5
S <sub>2</sub> RMS: cm	ERMS:3.6	N.	ERMS:4.4	N.	N.	ERMS:4.3
K <sub>1</sub> RMS: cm	ERMS:5.5	N.	ERMS:2.9	N.	N.	ERMS: 3.7
O <sub>1</sub> RMS: cm	ERMS:2.9	N.	ERMS:1.8	N.	N.	ERMS: 3.5

ARMS: amplitude RMS; ERMS: elevation RMS



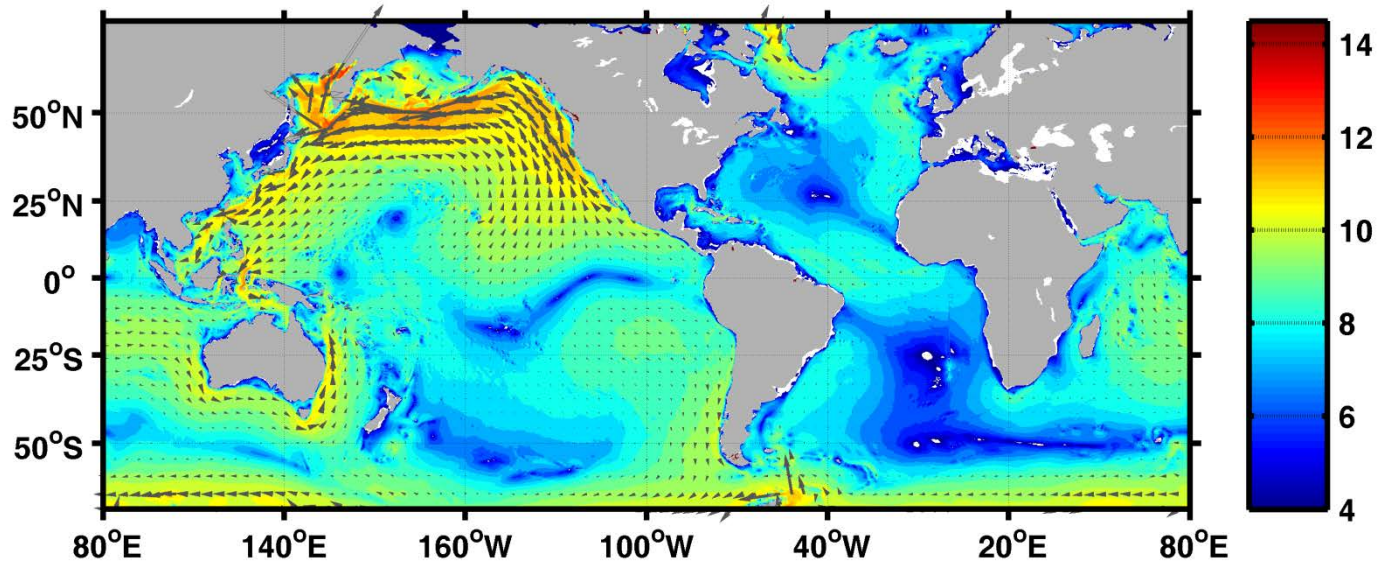


M<sub>2</sub> energy flux in TPX07.2, vectors represent the direction, color is the natural logarithm of the energy flux amplitude

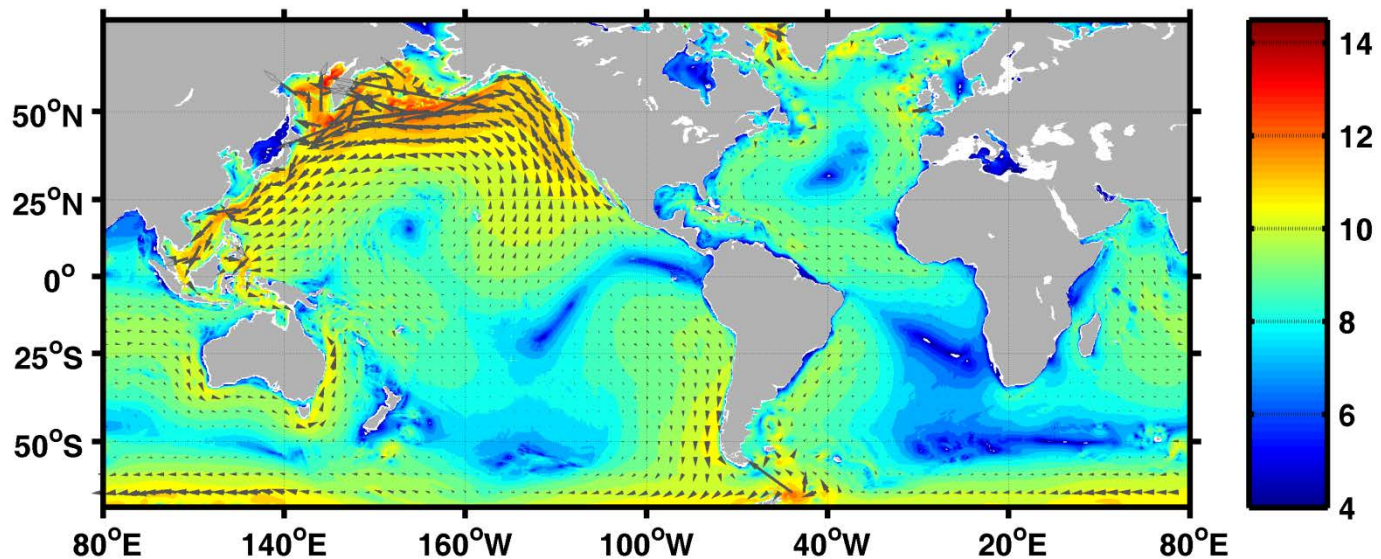


Same with above figure but for MOM4



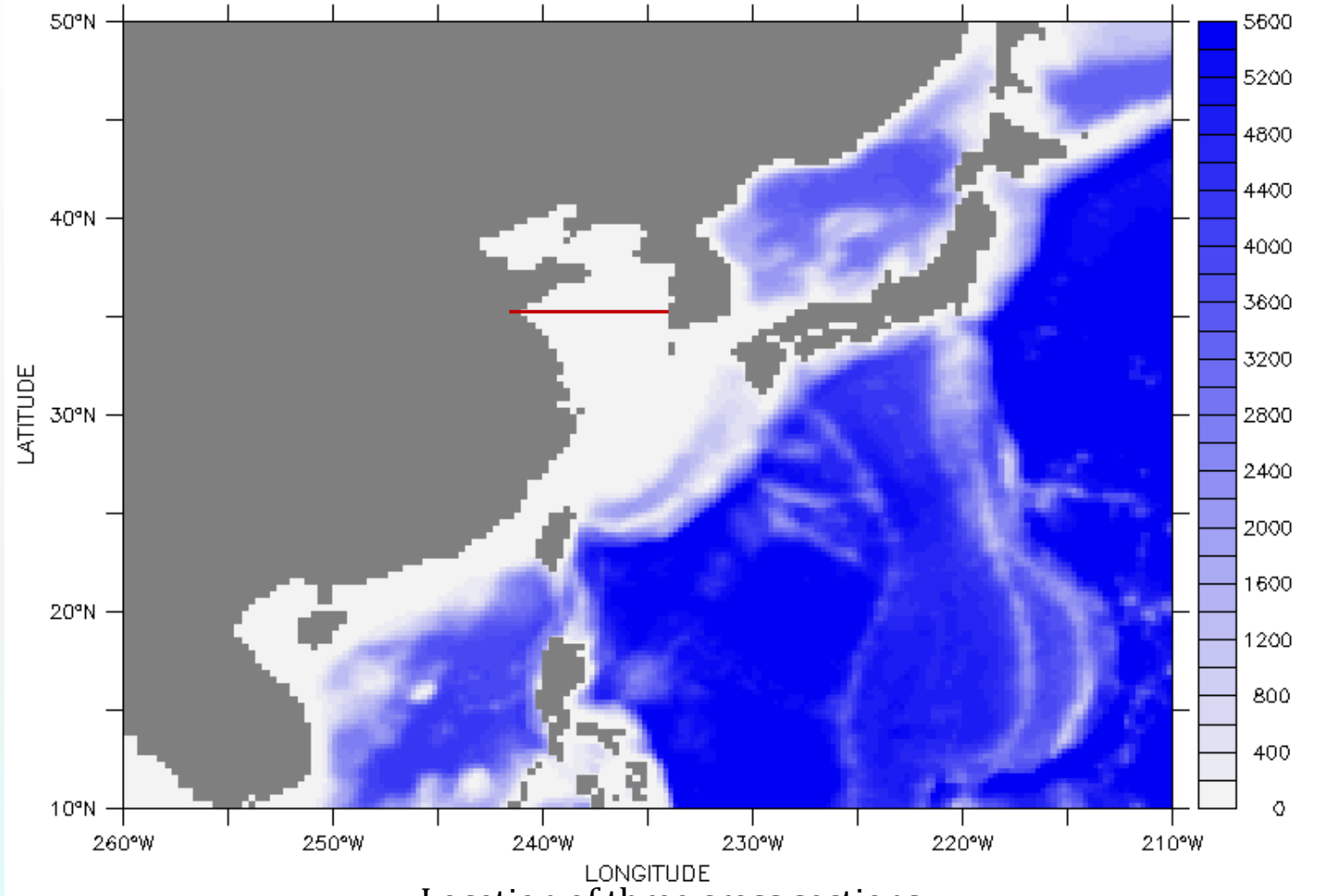


K<sub>1</sub> energy flux in TPX07.2, vectors represent the direction, color is the natural logarithm of the energy flux amplitude



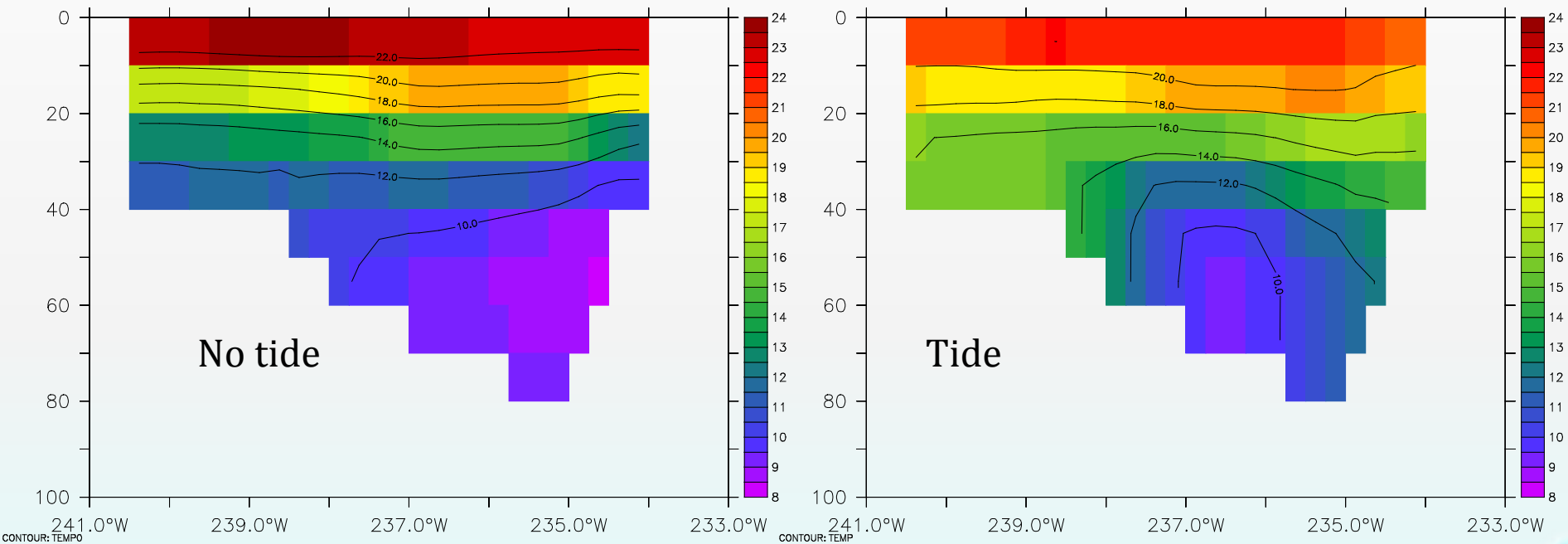
Same with above figure but for MOM4

# 5. Temperature at a glance



Location of three cross sections

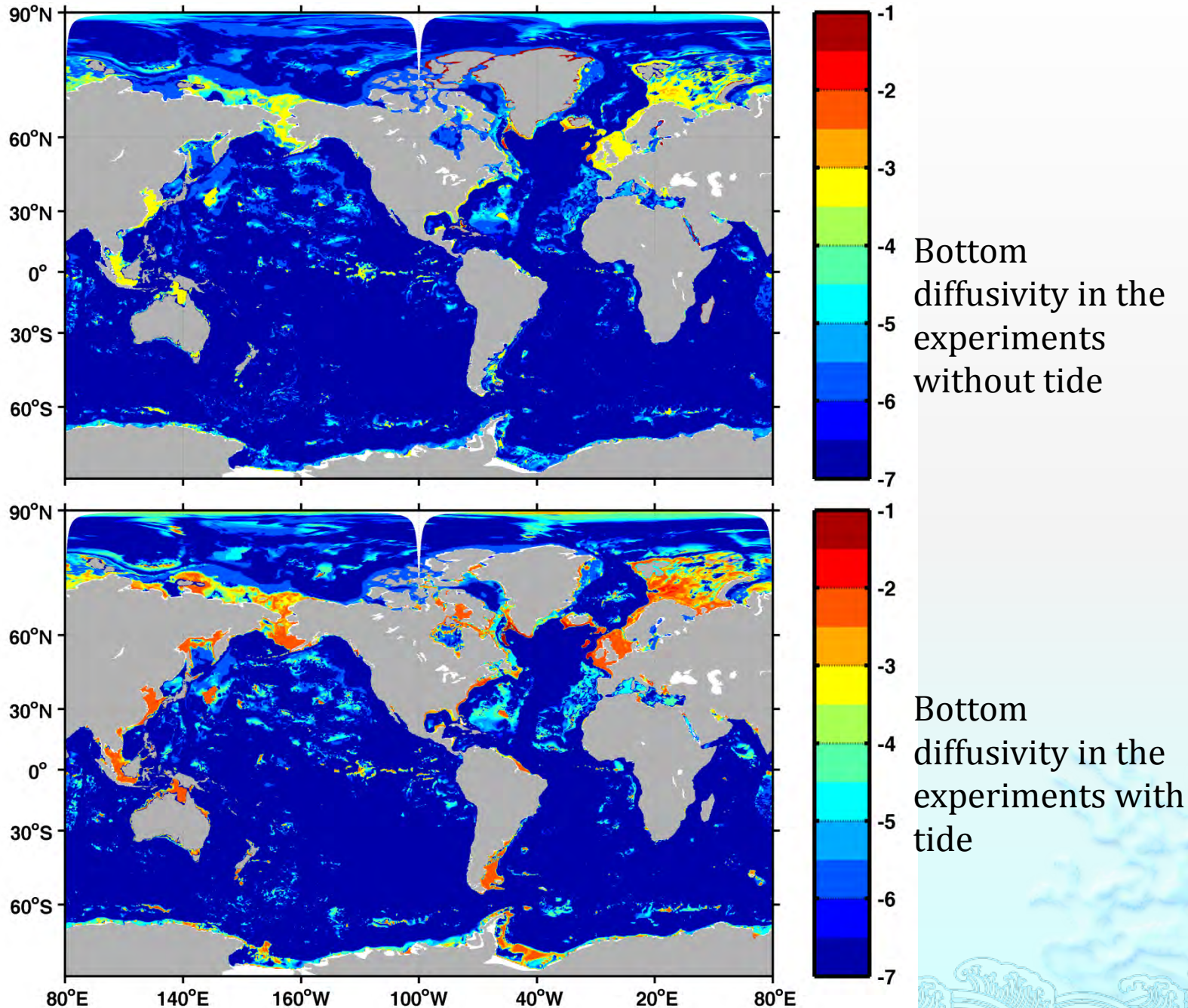
### 35°N cross section in the Yellow Sea, July monthly mean of 15th model year.



This results should be consistent with our previous regional model results, implying that tide is crucial for the formation of Yellow Sea cold water mass.



# Tidal influence on vertical diffusivity



## 6. Conclusions

- (1) With model topography constructed properly, sufficient horizontal resolution and inclusion of internal tide drag parameterization the Z-level ocean model is able to reproduce reasonably accurate global barotropic tide, the optimum ERMS errors of our model is 8.5cm.**
- (2) The preliminary result of the global tide-circulation coupled model show improved simulation in coastal region.**



**Thank s for your attention**

