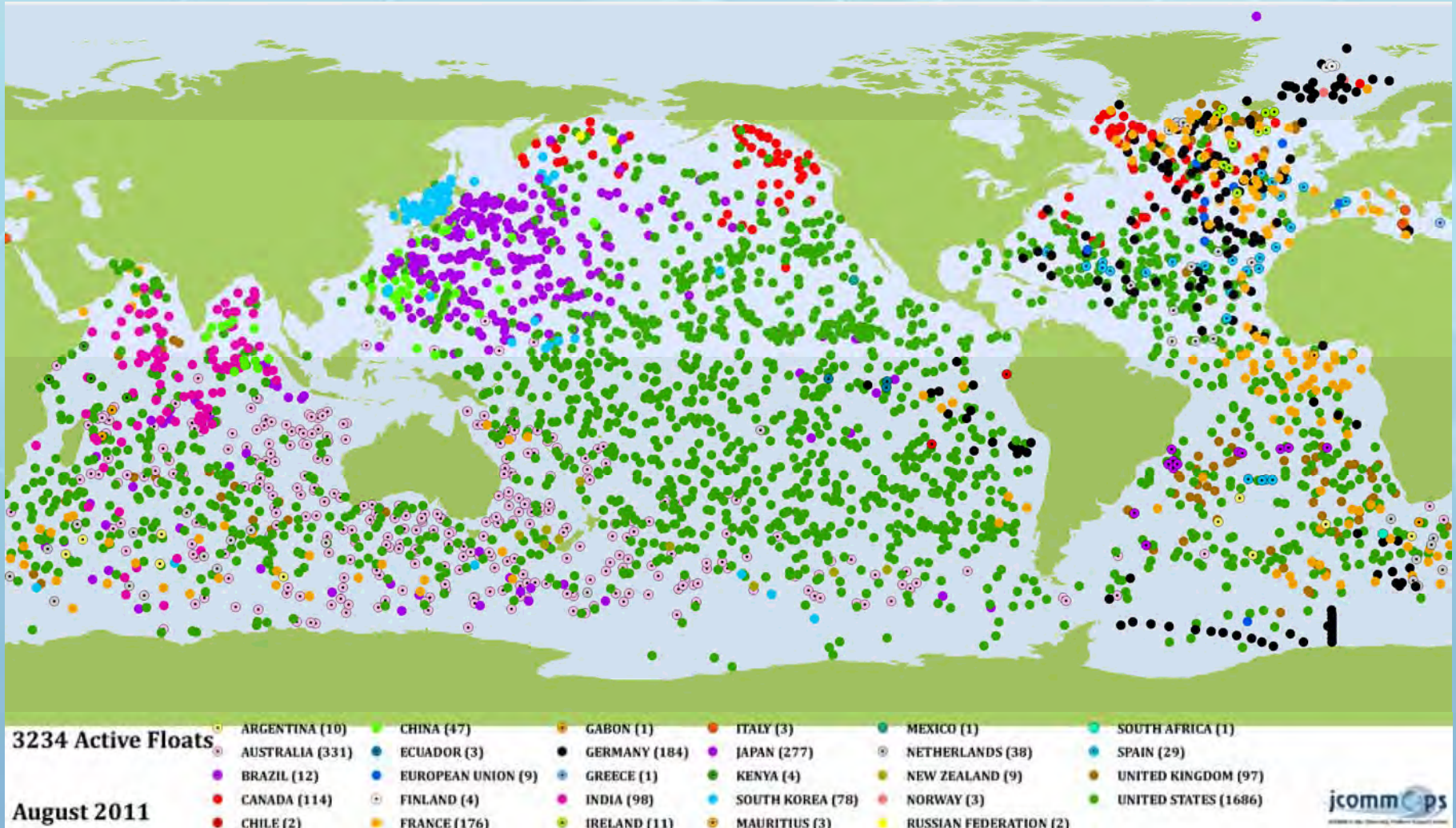


An analysis of the time-varying heat, salt and volume budget in an oceanic control volume

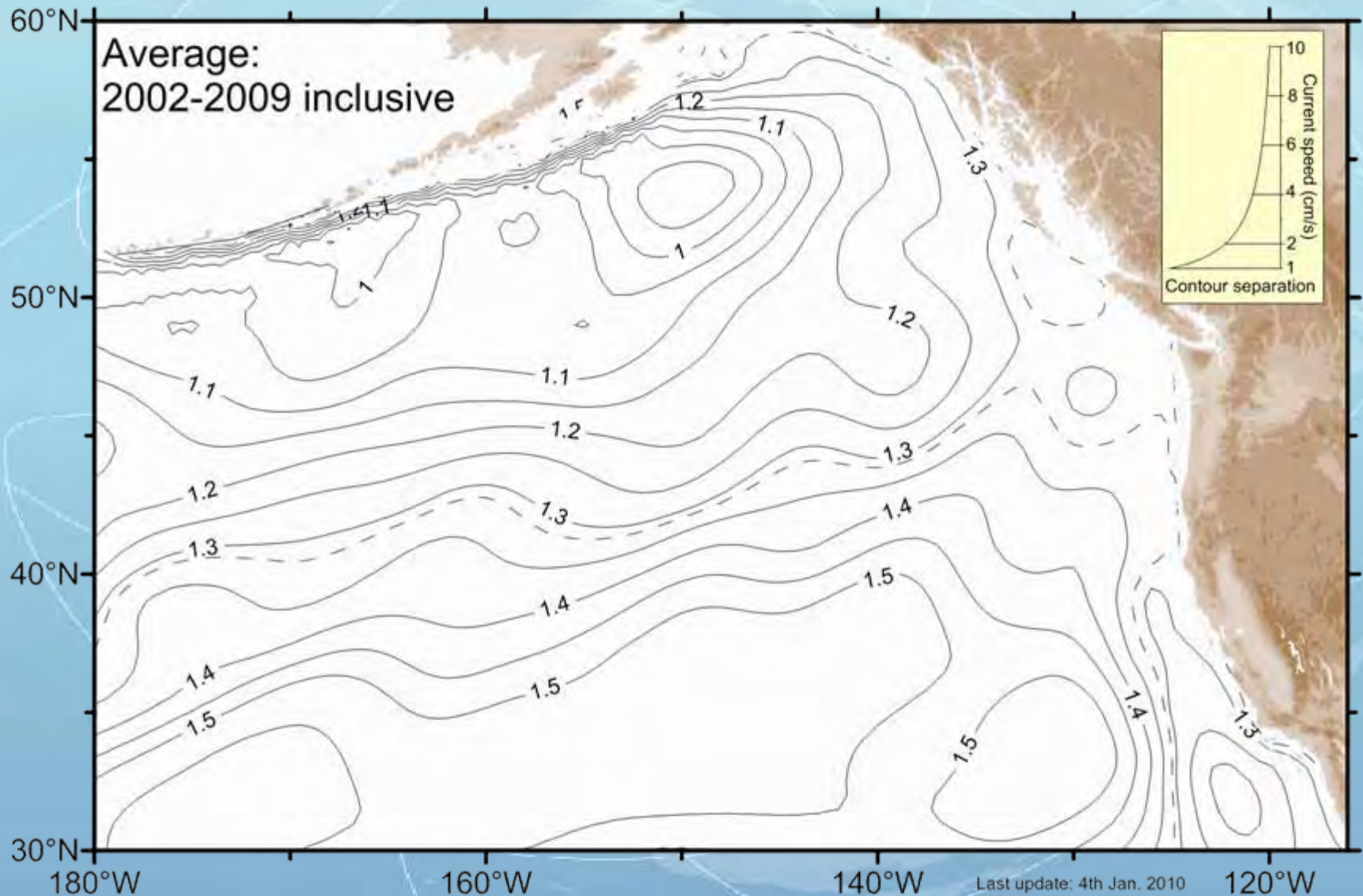
Howard Freeland
Institute of Ocean Sciences
howard.freeland@dfo-mpo.gc.ca

Lots of floats are in the water, and lots of countries contributing

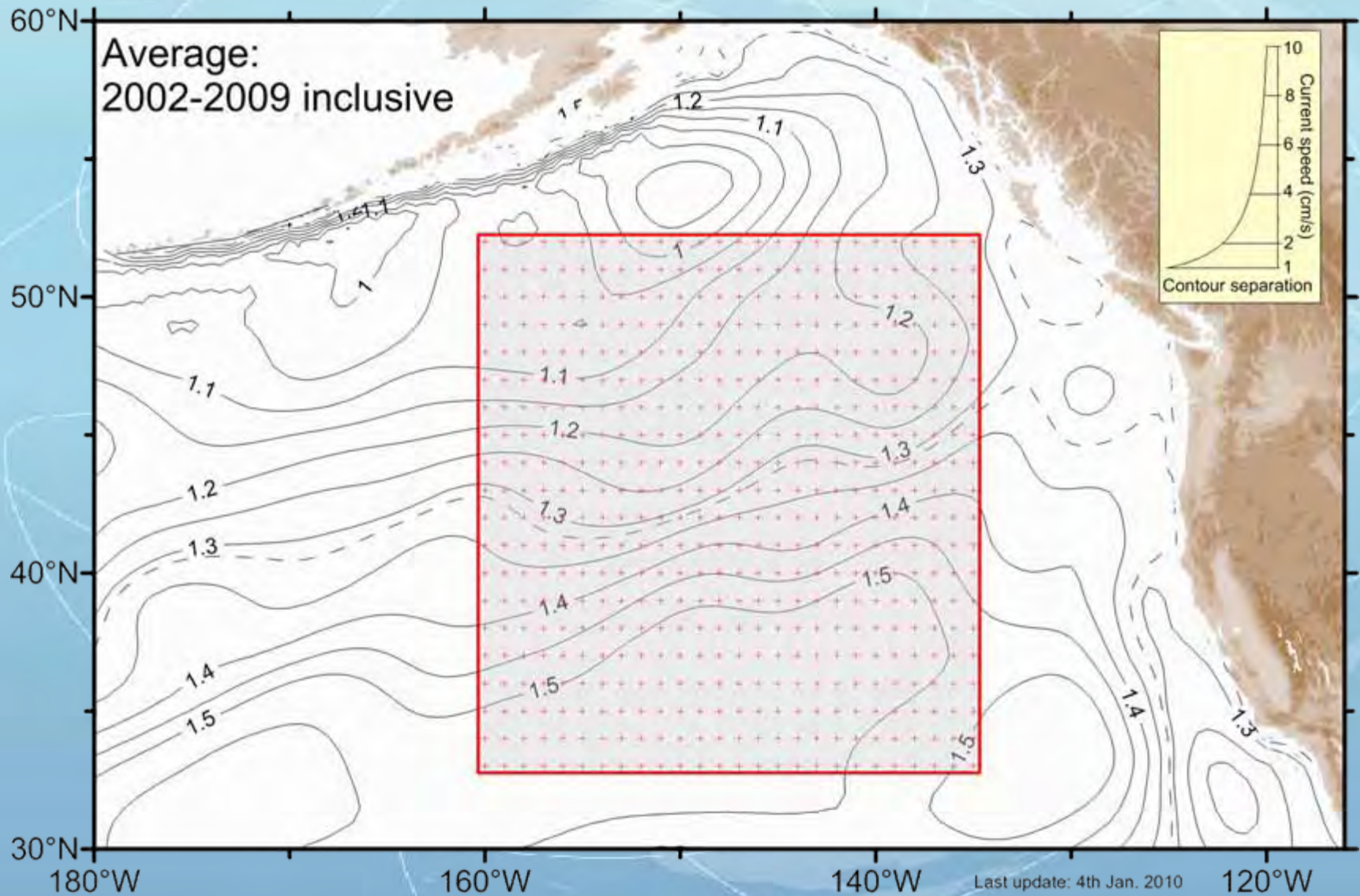


Can we determine the oceanic vertical velocity from this array?

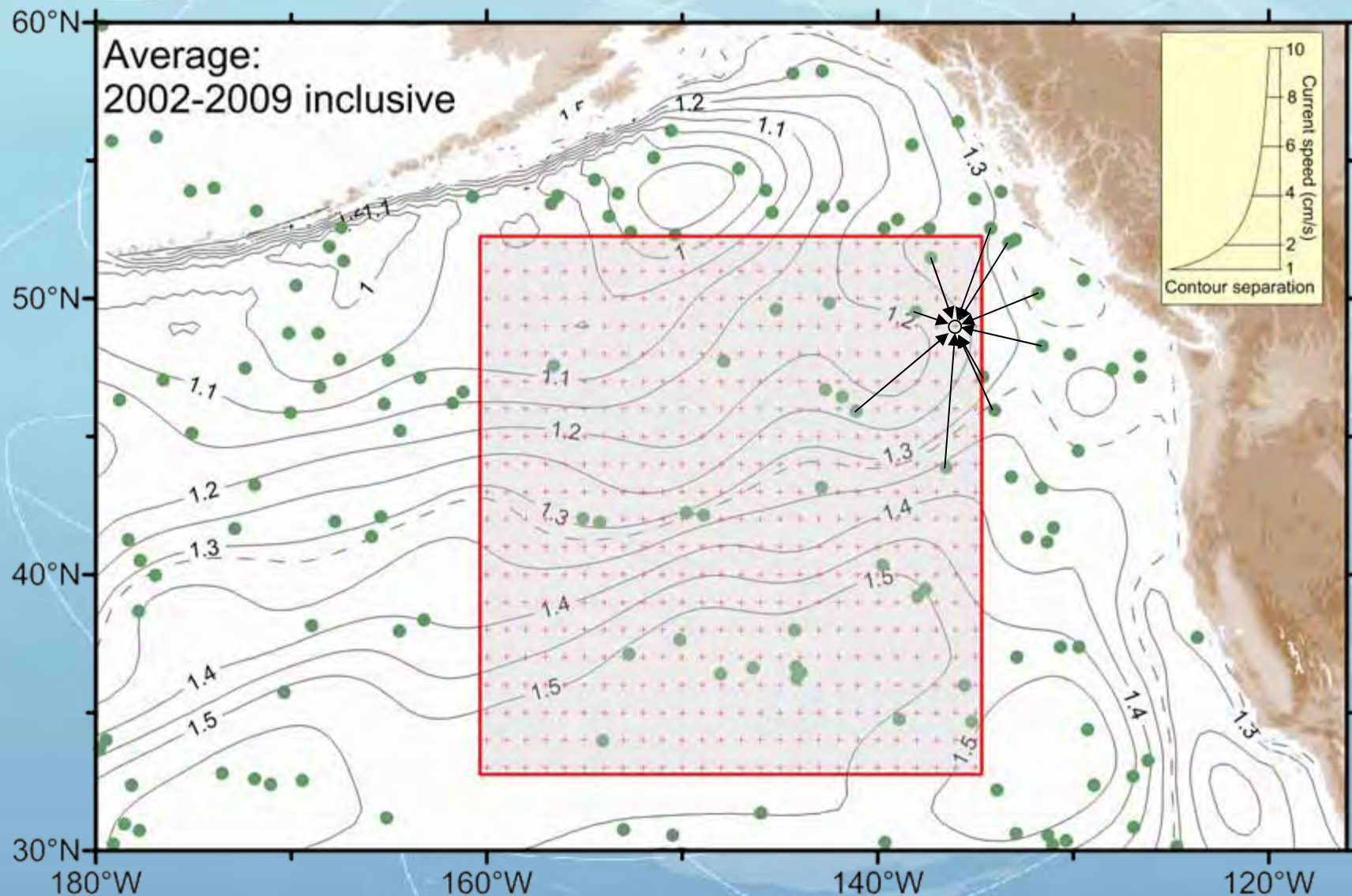
The mean circulation in the N. E. Pacific



The mean circulation in the N. E. Pacific



The mean circulation in the N. E. Pacific



Results for volume divergence of the mean state

$$\text{Divergence} = \langle \bar{u}_e \rangle - \langle \bar{u}_w \rangle + \langle \bar{v}_n \rangle - \langle \bar{v}_s \rangle$$

Relative to an integration pressure of 700 decibars:-

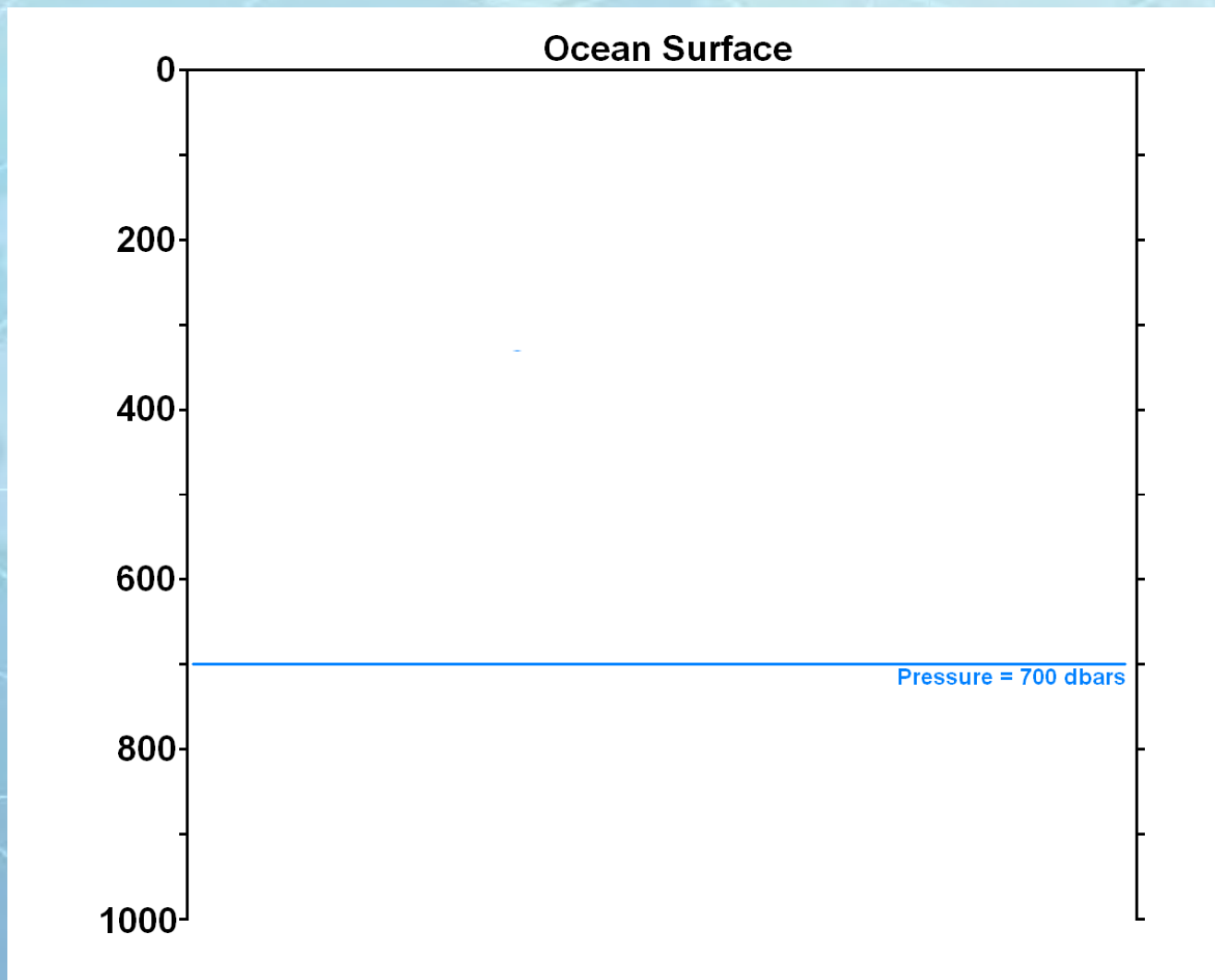
$$\text{Divergence} = 3.75 \times 10^6 \text{ m}^3 / \text{s} = \text{Area} \times w_{700}$$

$$\text{Hence:- } w_{700} = 8.85 \times 10^{-7} \text{ m/s}$$

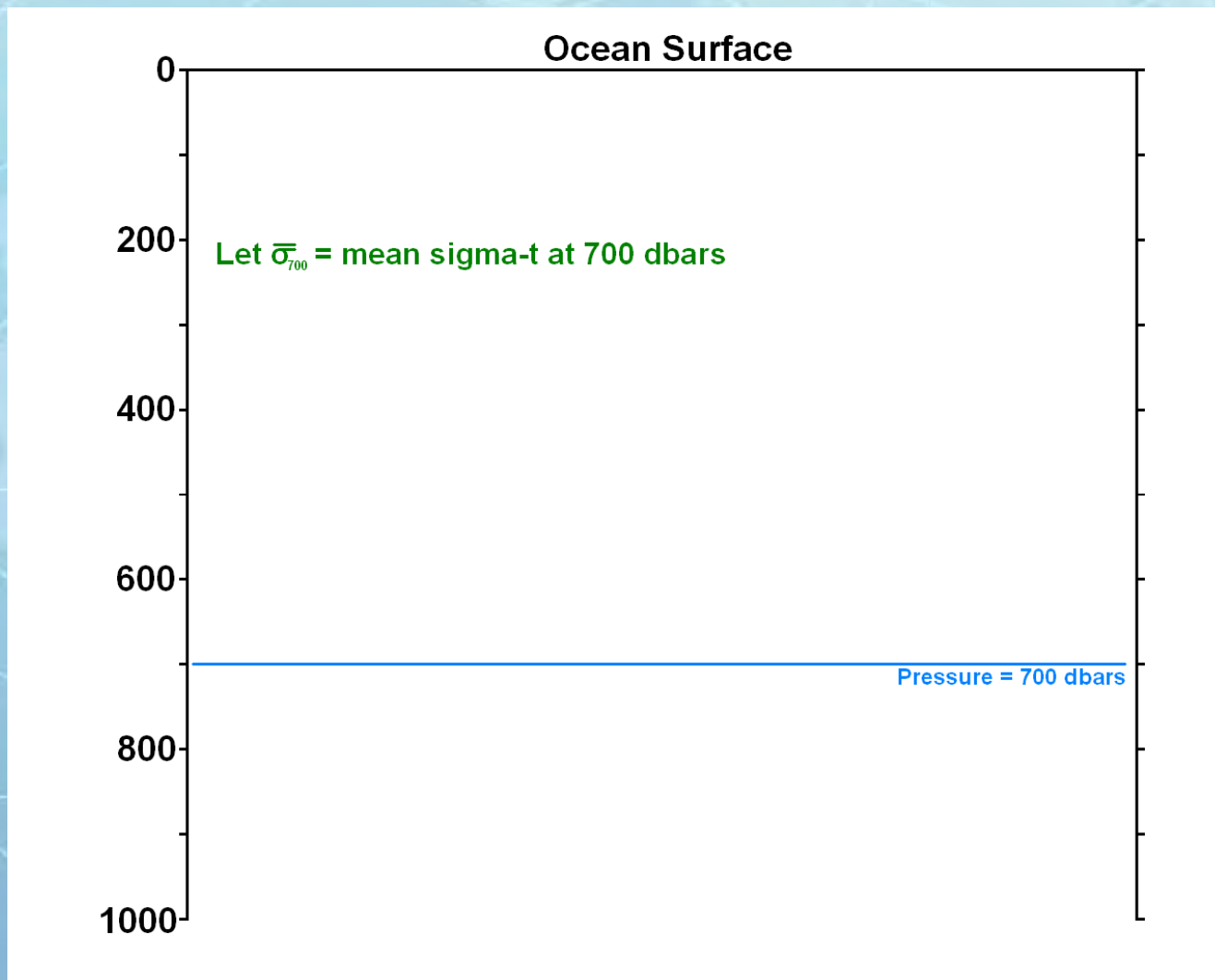
BUT – There are three components to this vertical velocity:

- 1) Diapycnal component
- 2) Isopycnal component
- 3) Heave

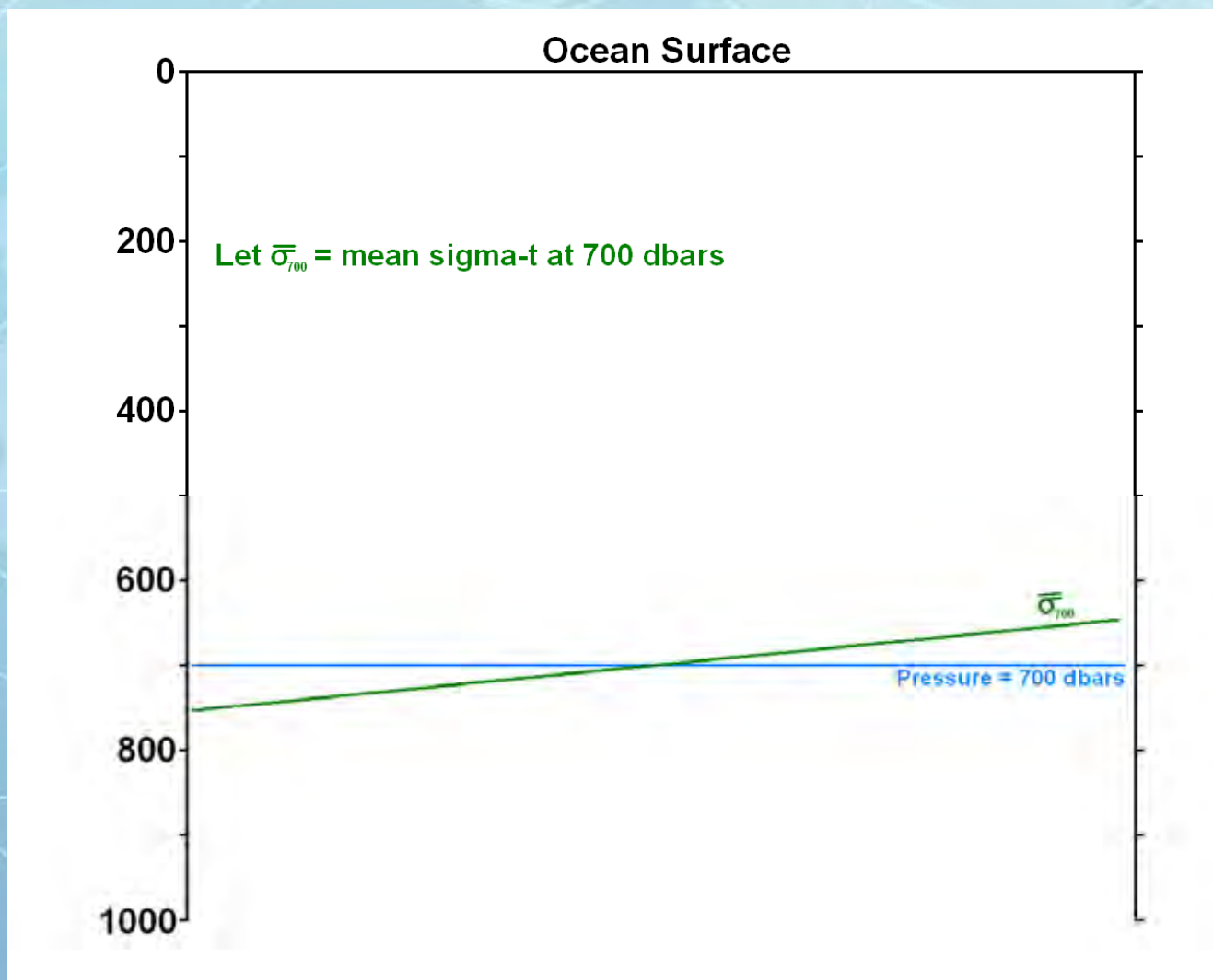
The three components of vertical velocity



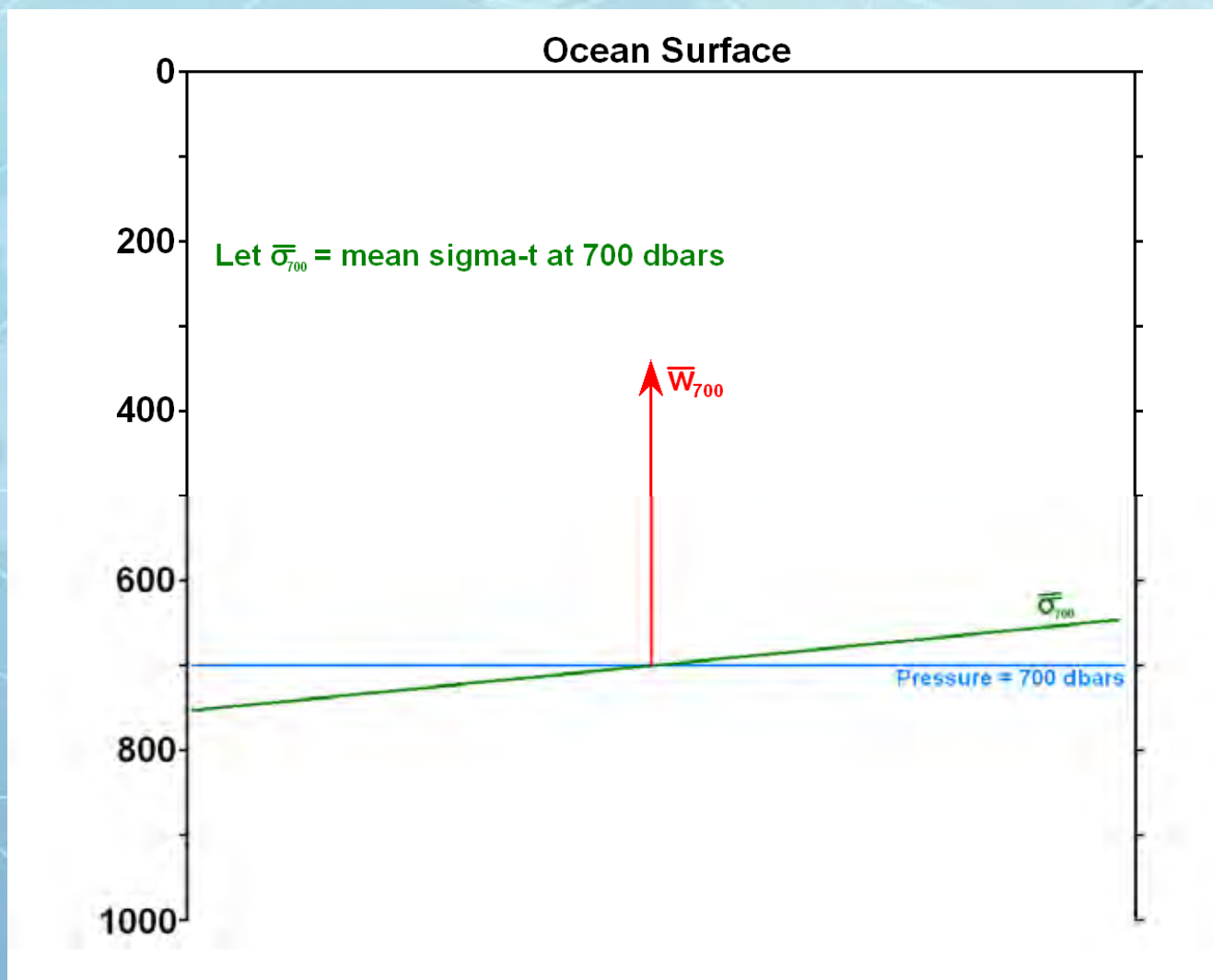
The three components of vertical velocity



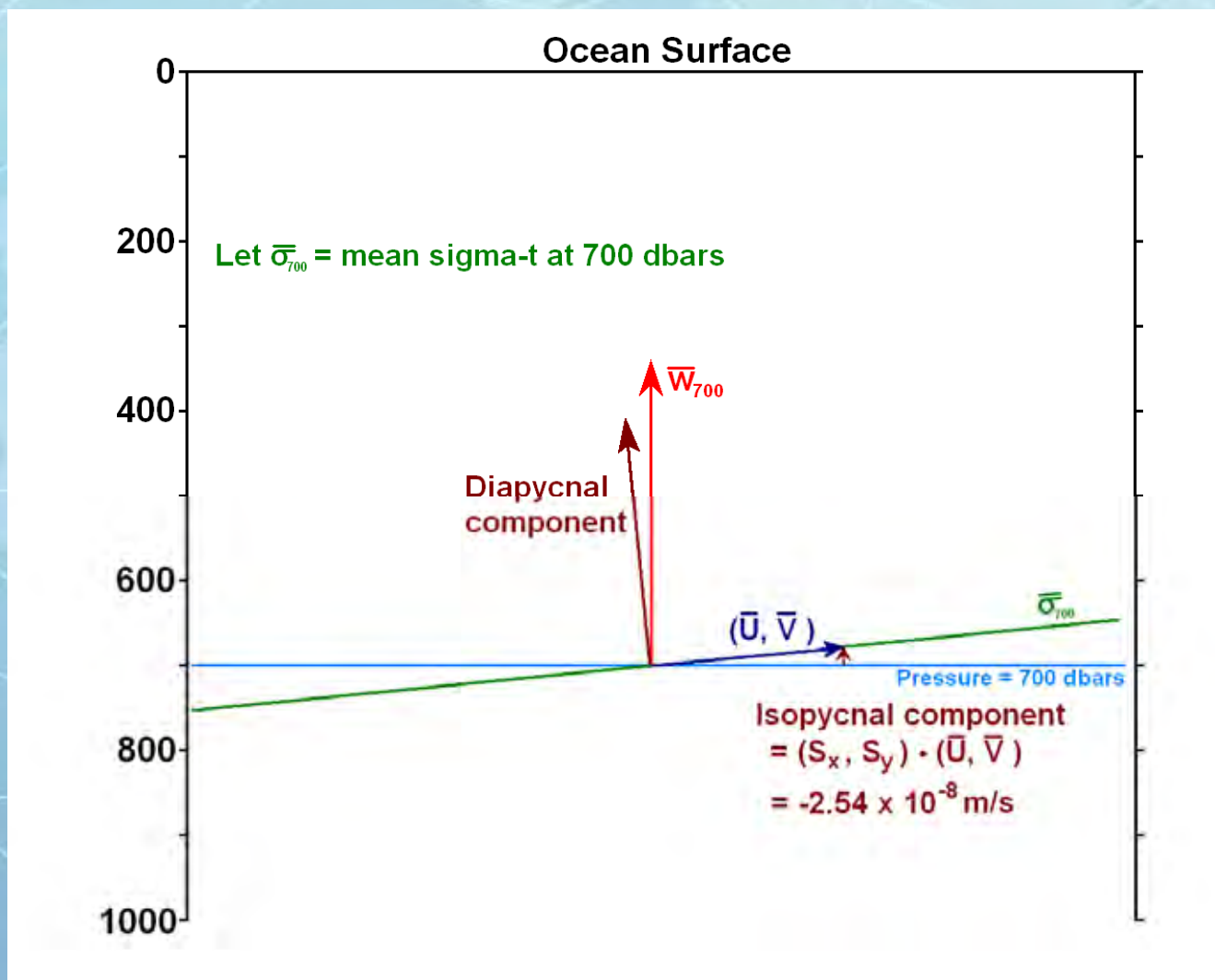
The three components of vertical velocity



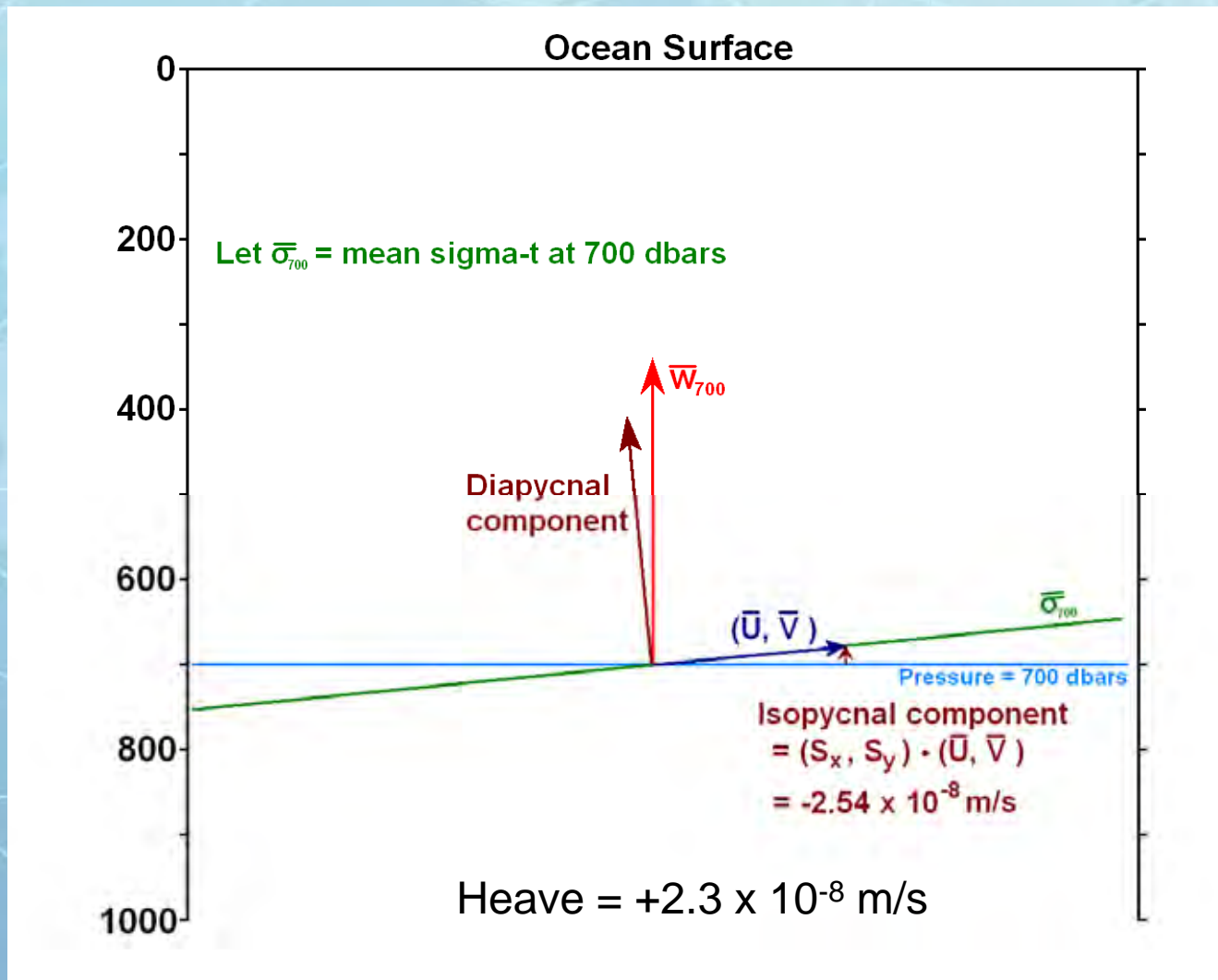
The three components of vertical velocity



The three components of vertical velocity



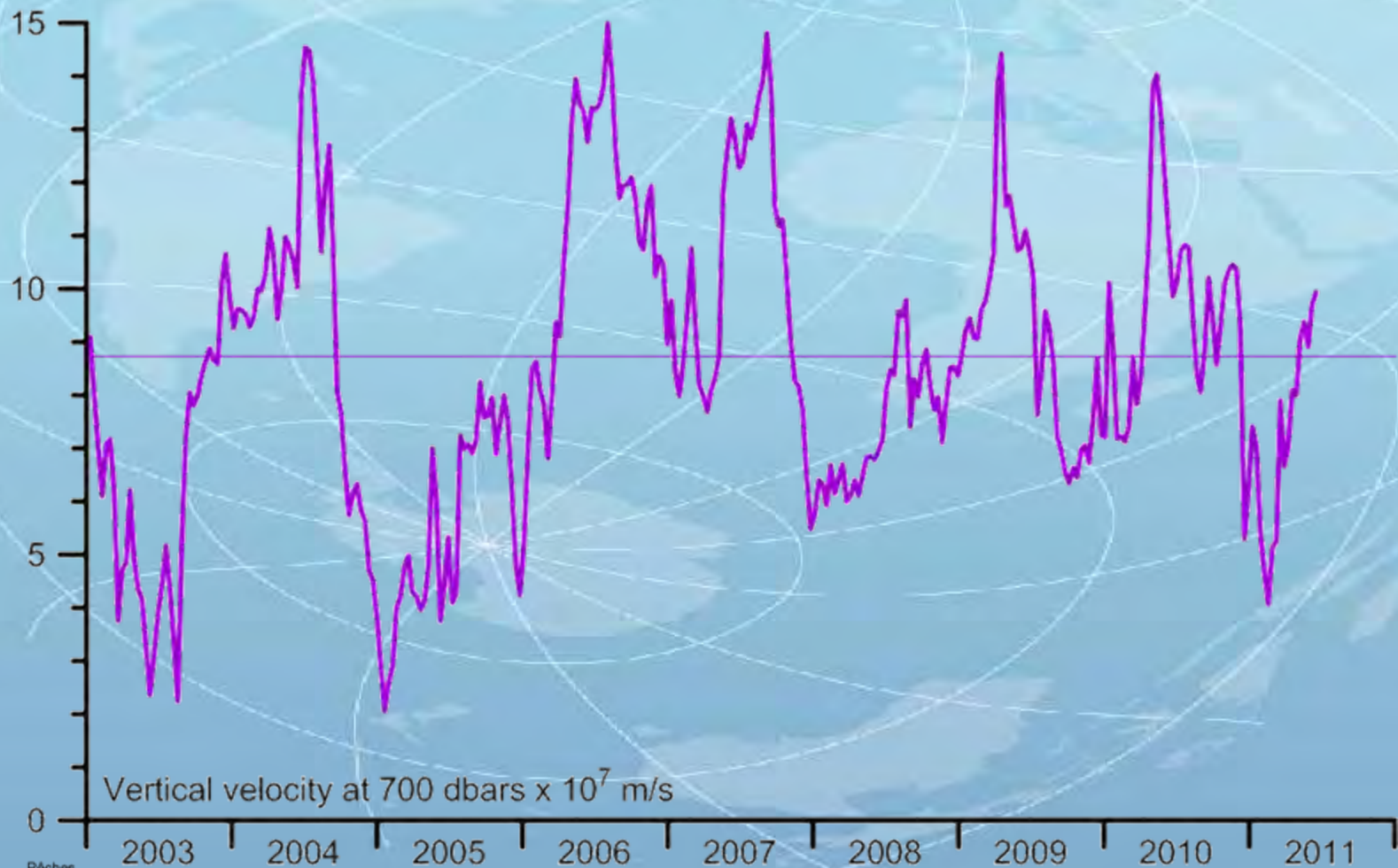
The three components of vertical velocity



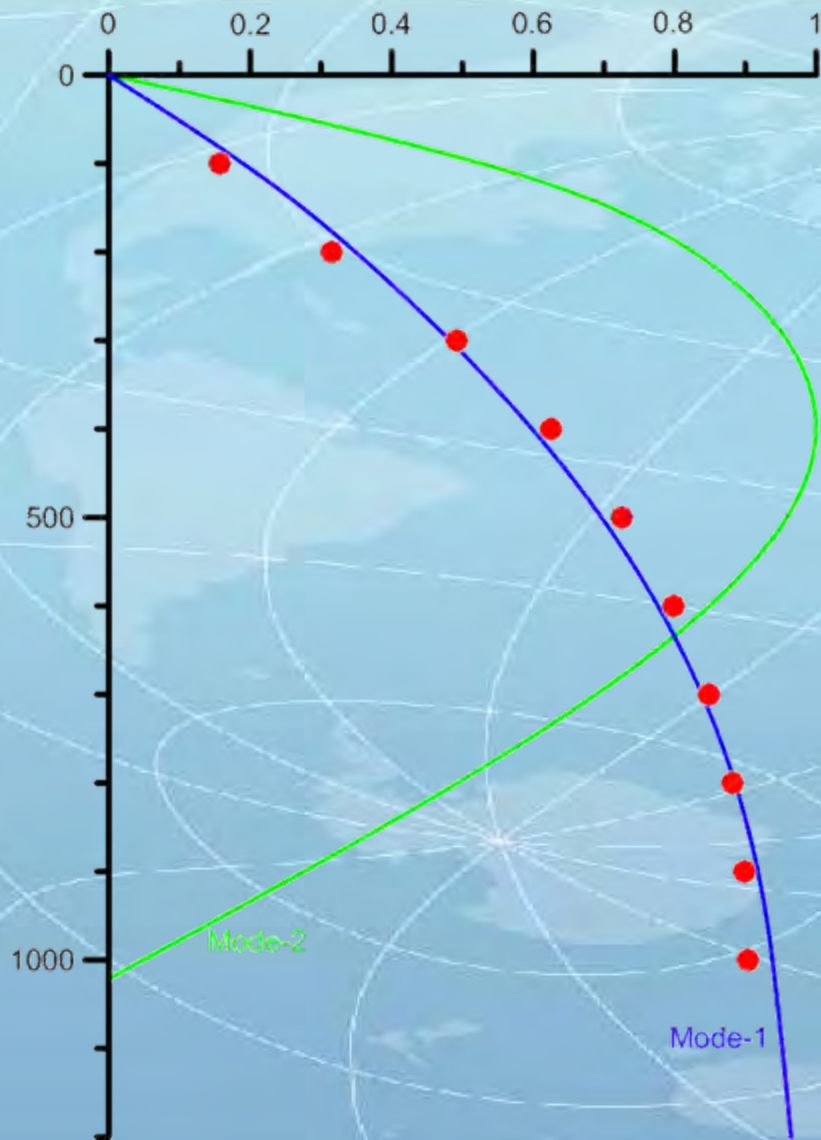
Results for volume divergence of the time-varying state

Relative to an integration pressure of 700 decibars:-

$$w_{700}(t) = (\langle u_e(t) \rangle - \langle u_w(t) \rangle + \langle v_n(t) \rangle - \langle v_s(t) \rangle) / Area$$



Plausibility test #1



The vertical structure of w estimates is extremely plausible.

Plausibility test #2 (mean state salt divergence)

$$\textit{Divergence} = \langle \bar{u}_e \bar{S}_e \rangle - \langle \bar{u}_w \bar{S}_w \rangle + \langle \bar{v}_n \bar{S}_n \rangle - \langle \bar{v}_s \bar{S}_s \rangle$$

$$\textit{Salt - Divergence} = +1.206 \times 10^8 \text{ psu.m}^3 / \text{sec}$$

Supply through the bottom surface = mean salinity on the 700 dbar surface x w_{700} (computed from volume budget) x Area

$$\textit{Supply} = +1.256 \times 10^8 \text{ psu.m}^3 / \text{sec}$$

Plausibility test #3 (mean state heat divergence)

$$\text{Divergence} = \langle \bar{u}_e \bar{H}_e \rangle - \langle \bar{u}_w \bar{H}_w \rangle + \langle \bar{v}_n \bar{H}_n \rangle - \langle \bar{v}_s \bar{H}_s \rangle$$

Where $H = \rho C_p T$ (C_p does vary with T and S)

$$\text{Heat} - \text{Divergence} = +1.279 \times 10^{11} \text{ J / sec}$$

Supply through the bottom surface = mean $\rho C_p T$ on the 700 dbar surface $\times w_{700}$ (computed from volume budget) \times Area

$$\text{Difference} = +0.69 \times 10^{11} \text{ J / sec}$$

To maintain the steady state we need to supply through the top surface 17.2 W/m².

Does this fit other estimates?

Annual mean heat flux 1950-1990

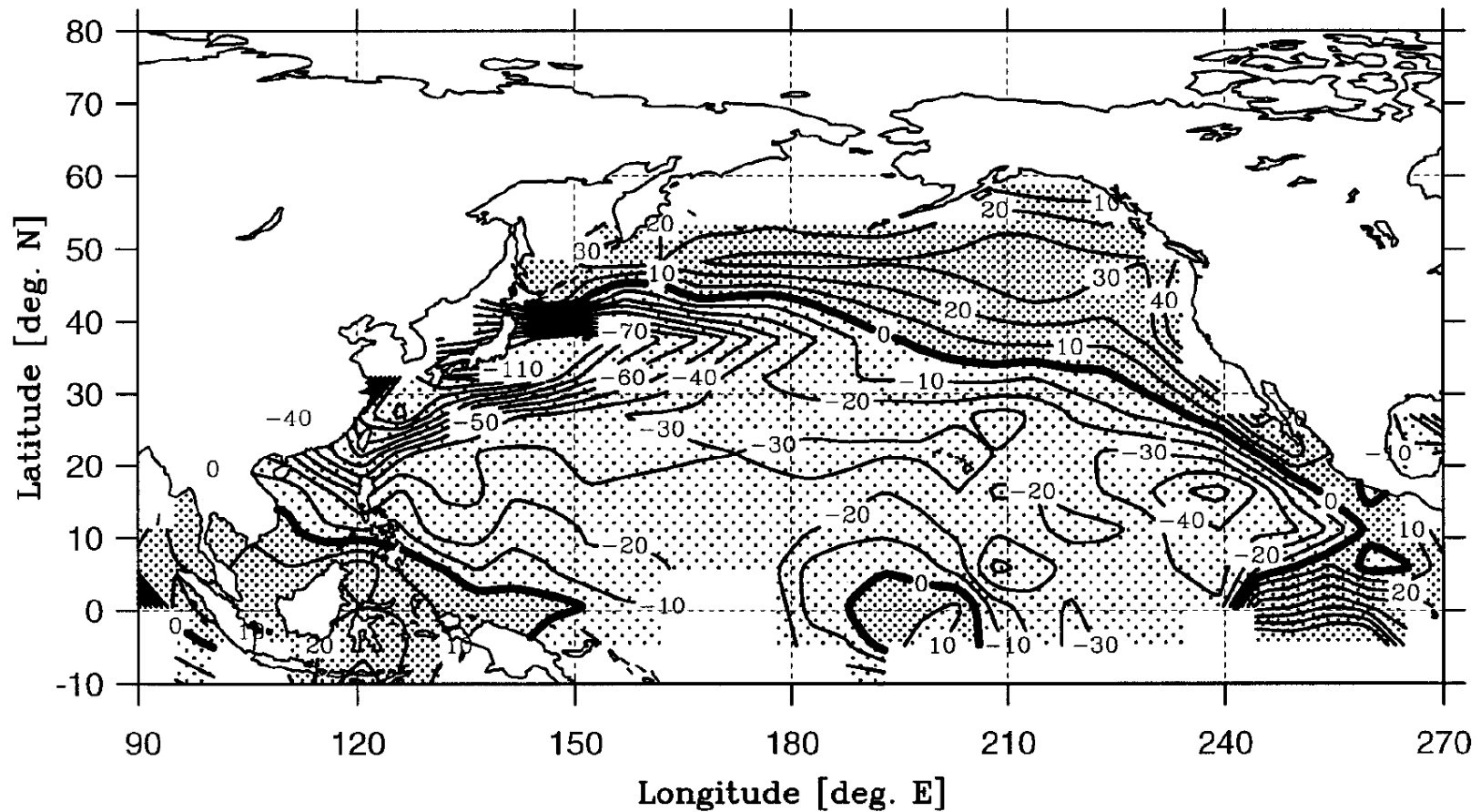


FIG. 11. The annual mean net heat flux between 1950 and 1990. Contour interval is $10 W m^{-2}$. Positive contours: solid line; negative contours: dashed line. Shaded region indicates where data was available.

Figure 11 from Moisan & Niiler, JPO 28, 401-421, 1998

Annual mean heat flux 1950-1990

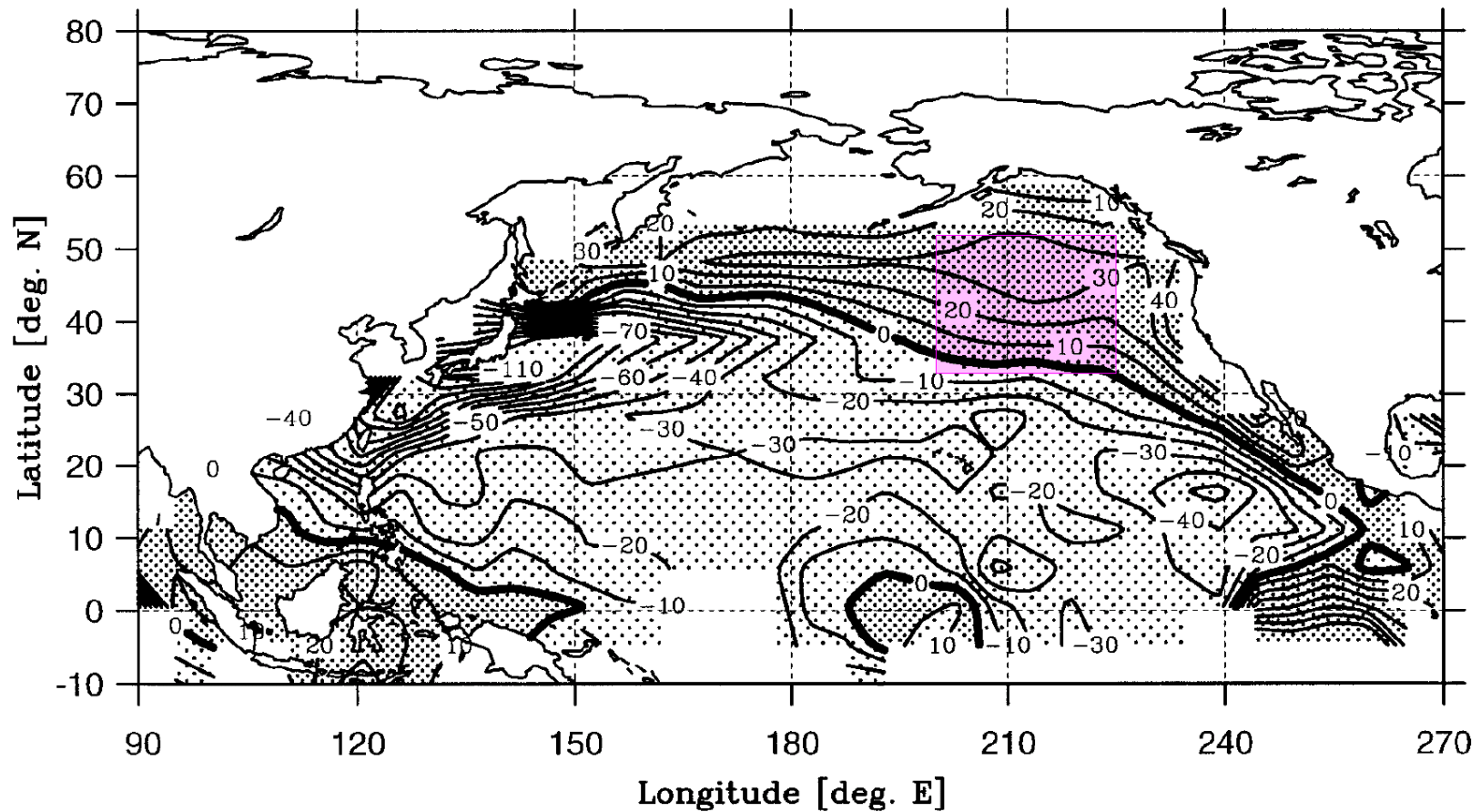


FIG. 11. The annual mean net heat flux between 1950 and 1990. Contour interval is $10 W m^{-2}$. Positive contours: solid line; negative contours: dashed line. Shaded region indicates where data was available.

Moisan & Niiler would suggest an expected annual average of about $25 \pm 10 W/m^2$

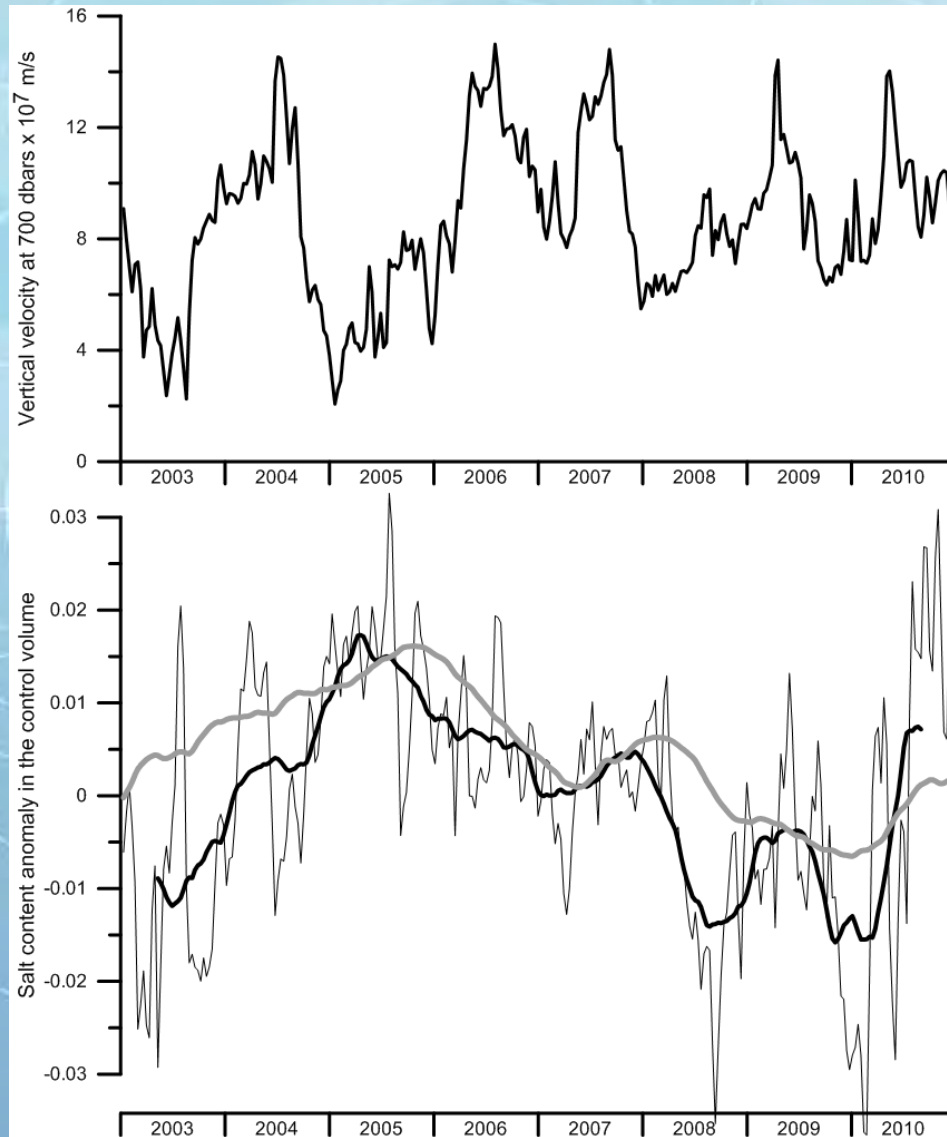
Plausibility test 4: Relationship between $w(t)$ and the time varying salt budget

$$\text{Let } \overline{\overline{S}}(t) = \frac{1}{V} \iiint S(x, y, P, t) dx \cdot dy \cdot dP$$

$$\text{and } \overline{S}'(t) = \overline{S}(t) - \frac{1}{T} \int_0^T \overline{S}(t) \cdot dt$$

$$\text{Then:- } \overline{S}'(t) = \frac{A_0}{V} \int_0^t w_{700}(\tau) \overline{S}_{700}(\tau) \cdot d\tau$$

Plausibility test 4: Relationship between $w(t)$ and the time varying salt budget



Implications for the main pycnocline

$$w \frac{\partial \rho}{\partial z} = \kappa \frac{\partial^2 \rho}{\partial z^2}$$

Which implies a simple solution in deep water:-

$$\rho(z) = \rho_0 + \Delta\rho \exp(-z / z_0)$$

Where $z_0 = \kappa/w$

By least-squares fit to the centre of the box,
between 300 dbars and 1000 dbars:-

$$z_0 = \kappa/w = 598 \text{ decibars}$$

$$\kappa = 5.3 \times 10^{-4} \text{ m}^2/\text{s}$$

Conclusions

- 1) Argo observations can be used to estimate large-scale heat, salt and volume budgets.
- 2) The volume budget of the geostrophic flow field implies a net upwelling velocity of about 8.9×10^{-7} m/s, this is overwhelmingly diapycnal.
- 3) The vertical velocity is highly variable, but can account for the large scale variations in salt content.
- 4) This w estimate implies a vertical diffusivity about 4 to 5 times larger than previous estimates, but there are no direct measurements. This might change soon, thanks to Jody Klymak.